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1 The added value of stochastic spatial disaggregation for short-term rainfall forecasts
2 currently available in Canada

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18 **Abstract**

19 Several businesses and industries rely on rainfall forecasts to support their day-to-day
20 operations. To deal with the uncertainty associated with rainfall forecast, some
21 meteorological organisations have developed products, such as ensemble forecasts.
22 However, due to the intensive computational requirements of ensemble forecasts, the
23 spatial resolution remains coarse. For example, Environment and Climate Change
24 Canada's (ECCC) Global Ensemble Prediction System (GEPS) data is freely available on
25 a 1-degree grid (about 100 km), while those of the so-called High Resolution
26 Deterministic Prediction System (HRDPS) are available on a 2.5-km grid (about 40 times
27 finer). Potential users are then left with the option of using either a high-resolution
28 rainfall forecast without uncertainty estimation and/or an ensemble with a spectrum of
29 plausible rainfall values, but at a coarser spatial scale. The objective of this study was to
30 evaluate the added value of coupling the Gibbs Sampling Disaggregation Model (GSDM)
31 with ECCC products to provide accurate, precise and consistent rainfall estimates at a
32 fine spatial resolution (10-km) within a forecast framework (6-hours). For 30, 6-h,
33 rainfall events occurring within a 40,000-km² area (Québec, Canada), results show that,
34 using 100-km aggregated reference rainfall depths as input, statistics of the rainfall fields
35 generated by GSDM were close to those of the 10-km reference field. However, in
36 forecast mode, GSDM outcomes inherit of the ECCC forecast biases, resulting in a poor
37 performance when GEPS data were used as input, mainly due to the inherent rainfall
38 depth distribution of the latter product. Better performance was achieved when the
39 Regional Deterministic Prediction System (RDPS), available on a 10-km grid and
40 aggregated at 100-km, was used as input to GSDM. Nevertheless, most of the analyzed

41 ensemble forecasts were weakly consistent. Some areas of improvement are identified
42 herein.

43 **Highlights**

- 44 • GSDM applied on reference data generates accurate and precise rainfall fields
- 45 • GSDM inherits the forecast bias
- 46 • Global ensemble forecasts (GEPS) are not consistent, with or without GSDM
- 47 • GSDM performance was better with regional deterministic forecasts (RDPS)
- 48 • Neighboring pixels should be considered when producing high-resolution
49 ensembles

50 **Keywords**

51 Gibbs Sampling Disaggregation Model (GSDM), Canadian Precipitation Analysis
52 (CaPA), Global Ensemble Prediction System (GEPS), Regional Deterministic Prediction
53 System (RDPS), ensemble, high-resolution rainfall.

54

55 **1 Introduction**

56 Numerous businesses and industries need consistent, precise and accurate, high-
57 resolution, short-term rainfall forecasts. For example, in urban areas, high-resolution
58 rainfall forecasts are of interest for stormwater management (*e.g.*, Gaborit *et al.*, 2014).
59 They are also important in rural areas where agricultural activities (*e.g.*, fungicide
60 applications, some herbicides applications, hay harvesting, manure application, irrigation
61 management), that are affected by local rainfall depth, require up-to-the-hour information
62 (*e.g.*, Cai *et al.*, 2007; Silva *et al.*, 2010; Cai *et al.*, 2011; Bendre *et al.*, 2015).

63 Thanks to advances in computational resources, understanding and parameterization of
64 key physical processes, increased access to satellite data, and data assimilation
65 techniques, meteorological models have made tremendous strides in the last decades
66 (Bauer *et al.*, 2015). One of the most spectacular changes that has occurred is an
67 impressive increase in horizontal resolution. For example, the horizontal resolution of
68 Environment and Climate Change Canada's (ECCC) global deterministic prediction
69 system has improved from approximately 150-km in 1990 to 25-km in 2013 (changes to
70 ECCC's operational model are documented at:
71 http://collaboration.cmc.ec.gc.ca/cmc/cmoe/product_guide/docs/changes_e.html).

72 Throughout Canada, deterministic forecasts are routinely issued on a grid having a
73 horizontal resolution of 2.5 km. The accuracy of the forecasts has improved accordingly.
74 For example, based on the root mean-squared-error (RMSE) of the 850 hPa temperature
75 forecasts issued by ECCC over North America, a 3-day forecast issued in 2015 was about
76 as accurate as a 1-day forecast issued in 1995, and a 5-day forecast issued in 2015 was
77 about as accurate as a 3-day forecast issued in 1995. This corresponds to a gain of

78 approximately one day of lead time per decade, which is consistent with improvements
79 reported by Bauer et al. (2015) for the European Centre for Medium-Range Weather
80 Forecasts.

81 Despite significant advances (e.g., COSMO forecast system; Baldauf *et al.*, 2011), it
82 remains difficult to get reliable rainfall forecasts for fine spatiotemporal scales. To
83 circumvent this issue, meteorological organisations are developing ensemble products
84 that provide several forecasts for a given timeframe; providing a spectrum of rainfall
85 depths associated with model uncertainty. However, because of the ensuing
86 computational requirements, the spatial resolution is generally coarser than that of a
87 deterministic run. Furthermore, outputs are not always made available on the original
88 model grid due to disk space constraints. For example, the Canadian ensemble forecasts
89 from the Global Ensemble Prediction System (GEPS) of ECCC, which are issued on a
90 50-km grid, are freely available on a 1-degree grid (about 100 km), while the spatial
91 resolution of their High Resolution Deterministic Prediction System (HRDPS) is about
92 40 times finer (2.5 km at 60°N). Thus, there is still a wide gap between available
93 forecasts and stakeholder requirements, namely: (i) rainfall estimates close to actual,
94 local-scale values, (ii) information about the uncertainty of local estimates, and for some
95 applications, (iii) available data for short-term decisions.

96 Meanwhile, rainfall and weather generators can both produce fine-scale rainfall fields
97 from coarse meteorological and/or climate simulations (e.g., Paschalis *et al.*, 2013; Peleg
98 and Morin, 2014; Niemi *et al.*, 2016). However, the goal of most applications is to
99 generate scenarios for long-term predictions. Alternatively, disaggregation models which

100 can generate rapidly several fine-scale rainfall fields from one coarse scale field represent
101 a promising avenue for short-term forecasts.

102 During the past decades, several studies have focused on spatial distribution of rainfall at
103 fine scale (Gupta and Waymire, 1993; Hubert *et al.*, 1993; Kumar and Foufoula-
104 Georgiou, 1993a,b; Marsan *et al.*, 1996; Olson and Niemczynowicz, 1996; among
105 others). An approach commonly used by disaggregation models is to divide in cascade
106 each grid cell in 2x2 pixels, which are then divided in 2x2 sub-pixels, so on so forth (*e.g.*,
107 Over and Gupta, 1996; Perica and Foufoula-Georgiou, 1996; Deidda, 2000; Harris and
108 Foufoula-Georgiou, 2001; Badas *et al.*, 2006; Deidda *et al.*, 2006a,b; Gaborit *et al.*, 2014;
109 among others). These models are conceptually simple, but may lead to unrealistic rainfall
110 fields with visible discontinuities, due to the discretization of the space (Lovejoy and
111 Schertzer, 2010a,b). Gagnon *et al.* (2012) proposed a stochastic disaggregation model,
112 hereafter referred to as the Gibbs Sampling Disaggregation Model (GSDM), which does
113 not produce discontinuities, even for adjacent pixels from two different grid cells (Figure
114 1). The model was adapted for orographic rainfall (Gagnon *et al.*, 2013) and used to
115 evaluate the impact of climate change on extreme rainfall events over a small watershed
116 (Gagnon and Rousseau, 2014). Nevertheless, the model has never been applied for short-
117 term meteorological forecasts.

118 The general objective of this study was to evaluate the capability of GSDM coupled with
119 ECCC products to provide accurate, precise and consistent rainfall estimates within a
120 short time frame. The specific objectives were to:

- 121 (i) Evaluate accuracy, precision and consistency of GSDM when applied on
122 aggregated reference rainfall fields;
- 123 (ii) Compare two freely-available ECCC rainfall forecasts, a deterministic and an
124 ensemble forecast, to a reference rainfall product (namely CaPA, *cf* Section 2.2);
- 125 (iii) Determine the added value of coupling GSDM to these ECCC forecasts;
- 126 (iv) Identify possible modifications to GSDM potentially leading to improved
127 forecasts.

128 This study focused on 30, 6-h, rainfall events that occurred between July and November
129 2015 over a 40,000-km² area on the south shore of the St. Lawrence River, Québec,
130 Canada.

131 **2 Materials and Methods**

132 **2.1 Study Area**

133 The region of interest consists of an area approximately 200 x 200 km², from 45 to 47° N
134 and from 71 to 73° W, covering the watershed of the Bécancour River on the south shore
135 of the St. Lawrence River in Québec, Canada (Figure 2). Primarily located in the St.
136 Lawrence Lowlands, only the upstream southeastern portion is in the Appalachian
137 Mountains. The climate is continental humid (Dfb under Köppen classification) with the
138 highest precipitation during the months of July, August and September. Around 40% of
139 the area, mainly in the Lowland sector, is occupied by agricultural activities that would
140 benefit from better local-scale rainfall forecasts. With respect to GSDM data
141 requirements, the modeled area spans from 44 to 48° N and from 70 to 74° W (study area
142 $\pm 1^\circ$ in each direction). In this manuscript, a grid cell refers to the spatial unit of a grid

143 with 1° (about 100-km) resolution and pixel refers to a spatial unit of a 10-km grid (see
144 Figure 2).

145 **2.2 Environment and Climate Change Canada products**

146 Three different ECCC products, all freely available on the web
147 (https://weather.gc.ca/grib/index_e.html), were used. First, the Canadian Precipitation
148 Analysis (CaPA; Fortin *et al.*, 2015) was identified as the reference (pseudo-observed)
149 precipitation. CaPA uses short-term forecasts as a background field and assimilates data
150 from various sources (stations, radars, satellites). The background field is modified by
151 spatial interpolation (kriging) of the difference between the forecast and the observations.
152 The dataset has a spatial resolution of 10 km x 10 km on a polar stereographic grid
153 covering North America. For this study, the computational domain consisted of a 40x40-
154 pixel grid (Figure 2) overlaying the area of interest (44-48°N and 70-74°W), oriented
155 east-west, by taking the closest pixel from the original grid.

156 Second, the Regional Deterministic Prediction System (RDPS; Caron *et al.*, 2015)
157 forecasts on the same grid as that of CaPA, similarly transposed on the 40x40-pixel grid
158 oriented east-west. It is important to note that RDPS provides the background field to
159 CaPA, the reference precipitation, and thus it could be an advantage for RDPS compared
160 to another product. That being said, the dense observation network and the radar in the
161 region analyzed provided sufficient data limiting the contribution of RDPS in CaPA. It is
162 thus assumed that the advantage of RDPS, if any, is negligible for the studied region.

163 The third and final product was the Global Ensemble Prediction System (GEPS; Charron
164 *et al.*, 2010; Houtemaker *et al.*, 2014) which produces 21 forecasts on a 1° x 1° (about
165 100 km x 100 km) grid. The 21 members are formed by one control member and 20

166 perturbed members, having different physical parameterization, data assimilation cycles
167 and initial observed conditions.

168 In addition to rainfall depth, three input atmospheric variables required by GSDM
169 (Section 2.3) were obtained from RDPS and GEPS forecasts: (i) convective available
170 potential energy (CAPE), (ii) wind speed and (iii) wind direction at the 700-hPa pressure
171 level.

172 CaPA and GEPS data are available at a 6-h time step, while RDPS data at a 3-h time step,
173 but aggregated at 6-h time step (sum for rainfall depth, average for wind speed and
174 CAPE). For GEPS, since simulations are launched twice a day, the required data covered
175 two forecast periods: (i) the first 6 hours and (ii) from 6 to 12 hours following the start of
176 the simulations. The same strategy is used for the RDPS, although RDPS forecasts are
177 available four times per day.

178 Two individual periods were analyzed for GSDM calibration and evaluation of rainfall
179 products. The calibration period covered May through October 2014 as well as May and
180 June 2015. Each CaPA grid point that received at least 1 mm of rain during a 6-h time
181 step was retained for calibration, for a total of 208,766 pixels. Atmospheric variables
182 (CAPE and wind at 700 hPa) were retrieved from RDPS forecasts. Evaluation of ECCC
183 products (Section 2.4) spanned from July to November 2015. A total of 30, 6-h time steps
184 with the largest mean GEPS forecasted accumulations were retained (Table 1).

185 Note that ECCC has other forecast products that could be of interest, but were not
186 included in the present study such as the High Resolution Deterministic Prediction
187 System (HRDPS; Mailhot *et al.*, 2010), having a 2.5-km resolution. Also, the Regional

188 Ensemble Prediction System (REPS; Charron *et al.*, 2013) having grid spacing of 15-km
 189 and a lead time of 72-h, with two integrations per day and 21 ensemble members, was not
 190 included since the data is not freely available. Moreover, it could be difficult to retrieve
 191 in a timely fashion for actual short-term forecasts.

192 **2.3 Gibbs Sampling Disaggregation Model (GSDM)**

193 The model assumed that $R_{i,j}$, the rainfall depth at a given 10-km pixel (i,j) for a given 6-h
 194 period, is a random variable with expected value μ and standard deviation σ given by
 195 (Gagnon, 2012; Gagnon and Rousseau, 2014):

$$196 \quad \mu = \bar{A} + \beta_d \left(\frac{A_{\downarrow} + A_{\uparrow}}{2} - \frac{A_{\leftarrow} + A_{\rightarrow}}{2} \right) + \beta_v V [\cos(2(W - 45^\circ))(A_{\leftarrow} - A_{\rightarrow}) + \cos(2(W - 90^\circ))(A_{\uparrow} - A_{\downarrow})]$$

197 (1)

$$198 \quad \sigma = (\beta_0 + \beta_1 C) \mu^{\beta_2} \quad (2)$$

199 where \bar{A} is the mean rainfall depth of the eight surrounding pixels and the other A 's are
 200 mean rainfall depths in the four directions, namely $A_{\downarrow} = \frac{R_{i-1,j-1} + R_{i+1,j+1}}{2}$,
 201 $A_{\uparrow} = \frac{R_{i-1,j} + R_{i+1,j}}{2}$, $A_{\leftarrow} = \frac{R_{i-1,j+1} + R_{i+1,j-1}}{2}$, and $A_{\rightarrow} = \frac{R_{i,j-1} + R_{i,j+1}}{2}$, V is the 700-hPa
 202 wind speed (m/s), W is the 700-hPa wind direction (degree), C stands for CAPE (J/kg),
 203 and the five calibration parameters are: β_d (dimensionless), β_v (s/m), β_0 (mm), β_1 (mm
 204 kg/J), and β_2 (dimensionless). As in many rainfall models (*e.g.*, Over and Gupta, 1996;
 205 Fiorucci *et al.*, 2001; Forman *et al.*, 2008; Groppelli *et al.*, 2011), a lognormal
 206 distribution is assumed for $R_{i,j}$. In these equations, it is assumed that strong 700-hPa

207 winds might lead to anisotropy and high CAPE values increase spatial variability (*i.e.*,
208 decrease the influence of the neighboring pixels).

209 The model can disaggregate at any spatial resolution, but it is recommended to target a
210 resolution at which rainfall depths are available for calibration. In this study, 10-km 6-h
211 rainfall depths from 208,766 pixels from CaPA analyses were used for calibration
212 (Section 2.2). The estimated values for parameters β_d and β_v of Equation (1) minimizes
213 the sum of the squared differences between observed rainfall depths and expected rainfall
214 depths calculated using Equation (1) for all pixels used for calibration (Gagnon, 2012;
215 Gagnon *et al.*, 2012). Then, groups were created from all calibration pixels; all pixels
216 within a group had similar expected rainfall depths and CAPE values. For each group,
217 mean expected rainfall depth and mean CAPE value were calculated. The estimated
218 values for parameters β_0 , β_1 , and β_2 of Equation (2) minimizes the sum of the squared
219 differences between the observed 99.9% quantile of rainfall depths in each group and the
220 99.9% quantile calculated using the lognormal distribution with mean expected rainfall
221 depth for each group and standard deviation given by Equation (2) (with mean CAPE
222 value for each group and calibration parameters). Fitting the 99.9% quantile was done to
223 attenuate the underdispersion of the lognormal distribution for rainfall depth estimation
224 (Gagnon *et al.*, 2012; Gagnon and Rousseau, 2014).

225 Equations (1) and (2) allow rainfall depths to be generated on a 10-km pixel when
226 neighboring depths are known. However, in practice, only coarse scale (100 km in this
227 study) data is available as input to the disaggregation model. An algorithm based on the
228 Gibbs sampling theory (Geman and Geman, 1984; Roberts and Smith, 1994) was
229 developed to circumvent this issue. First, as initial conditions, the rainfall depth for each

230 10-km pixel was set to the rainfall depth of the 100-km grid cell covering the pixel. Then,
231 new rainfall depths were generated from the lognormal distribution using Equations (1)
232 and (2) for each 10-km pixel, one at the time. An *iteration* is completed when all pixels
233 have been updated once. After each iteration, a multiplicative factor (generally close to 1)
234 was applied to ensure that the model preserved the exact rainfall depth of each 100-km
235 grid cell used as input. Based on the Gibbs sampling theory (Geman and Geman, 1984;
236 Roberts and Smith, 1994), the rainfall depth on each 10-km pixel is approximately
237 distributed using the lognormal distribution along with Equations (1) and (2) after a
238 sufficient number of iterations. In this study, 300 iterations were performed before
239 retaining the first disaggregated rainfall field, referred to as the first *realization*. Since
240 fields from consecutive iterations are autocorrelated, subsequent realizations were
241 separated by 100 iterations. The model is not explicitly made to generate spatial rainfall
242 intermittency (*i.e.*, pixels without rain), but this can be achieved by setting to 0 those
243 rainfall depths below a given threshold (0.1 mm in the present work). A detailed
244 description of the algorithm is provided in Gagnon (2012), Gagnon *et al.* (2012) and
245 Gagnon and Rousseau (2014).

246 **2.4 Products analyzed**

247 For each one of the 30, 6-h, rainfall events retained (Section 2.2), a total of 13 different
248 rainfall products were analyzed (Table 2). These products were referenced with respect to
249 the ECCC product used (“C” for CaPA analyses, “R” for RDPS forecasts and “G” for
250 GEPS forecasts), whether aggregation and/or disaggregation was performed (“d” for 10-
251 km disaggregated product, “a” for 100-km aggregated product without disaggregation),
252 and whether neighboring pixels were used to create an ensemble (“n” if so).

253 The original 10-km CaPA rainfall (C) became the reference (true value) for the 12 other
254 series. GSDM was first applied with aggregated CaPA data (Ca) as input. The ensuing
255 product (Cd) compared to the reference (C) evaluates the performance of the
256 disaggregation model. Comparison of the outcomes of Cd with Ca was used to assess the
257 added value of GSDM over a low-resolution product.

258 One of the strength of GSDM is that it can generate realistic spatial patterns, even with
259 100-km grid cells used as input. However, it cannot always be right at the exact location
260 (10-km pixel) since no fine scale information is used as input. Thus, it was decided to
261 evaluate another disaggregated ensemble product, which instead of considering only the
262 rainfall depths generated at the target pixel (as for Cd), it also includes the rainfall depths
263 in the neighboring area (Cdn; 100 model realisations x 121 pixels [+/- 5 pixels in each
264 direction] = 12,100 rainfall depths per 10-km pixel per 6-h event). The ensembles Cd and
265 Cdn were also compared with the ensemble formed by the CaPA rainfall depths in 120
266 neighboring pixels (+/- 5 pixels in each direction - the target pixel; Cn, Table 2). This
267 latter ensemble was used to evaluate whether neighboring pixels could actually be used
268 for suitable estimation of the rainfall depth of the target pixel in this area.

269 Eight forecast products were compared. For both RDPS and GEPS forecasts, analyses
270 were performed on rainfall depths from raw products (referred to as R and G,
271 respectively), in order to evaluate the actual forecasts available for an end user. Then,
272 disaggregation at the target pixel (Rd and Gd) and disaggregation in the neighboring area
273 (Rdn and Gdn) was performed to evaluate the added value of GSDM coupled with the
274 forecasts. For RDPS, it required data aggregation (Ra) prior disaggregation. For a given
275 pixel, RDPS outcomes in the neighboring area (+/- 5 pixels in each direction; Rn) were

276 also analyzed. The interest in R_n lies in the construction of an ensemble from a
277 deterministic forecast requiring no additional computational time, contrary to
278 disaggregation.

279 **2.5 Performance evaluation**

280 The performance of a product was assumed to vary depending on the reference rainfall
281 depth (large rainfall depths being more difficult to correctly place spatially) and on the
282 type of events (stratiform or convective events being governed by different physical
283 processes). Seven groups, based on these two variables, were constructed (Table 3) and
284 performance metrics calculated independently for each group.

285 Three criteria were accounted for in the evaluation: accuracy, precision and, for
286 stochastic products only, consistency. Accuracy refers to bias, that is the mean difference
287 between simulated and observed values. Precision is defined in two ways. Precision of a
288 probabilistic product is related to the variability (range) of the realizations. Precision of
289 the error, for a deterministic or probabilistic product, is related to the variability of the
290 difference between the prediction and the reference. Finally, consistency is when the
291 reference value is indistinguishable from a randomly selected member of an ensemble
292 (Anderson, 1997).

293 For all products, deterministic or probabilistic, the Mean Squared Error (MSE) was
294 calculated. For a given group with n pixels (Table 3) and a given rainfall product, let $x_1,$
295 \dots, x_n be the reference rainfall depths (C; Table 2) and y_1, \dots, y_n be the corresponding
296 forecasted rainfall depths from the product. If the product is probabilistic, the mean
297 forecast for each pixel was calculated to allow a comparison with deterministic products.

298 That is, $y_i = \sum_{j=1}^{n_r} \frac{y_{i,j}}{n_r}$ where n_r is the number of probabilistic realizations (members) and $y_{i,j}$
 299 is the simulated rainfall depth for j^{th} realization at the i^{th} pixel. The MSE was calculated
 300 as follows:

$$301 \quad \text{MSE} = \sum_{i=1}^n \frac{(y_i - x_i)^2}{n} = \sum_{i=1}^n \frac{((y_i - x_i) - (\bar{y} - \bar{x}))^2}{n} + (\bar{y} - \bar{x})^2 \quad (3)$$

302 The two terms on the right-hand side of the equation correspond to the variance of the
 303 error (precision of the error) and the squared of the bias (accuracy), respectively.

304 For probabilistic products only, the Cumulative Rank Probability Score (CRPS;
 305 Matheson and Winkler, 1976) was calculated for each ensemble product and each group
 306 (Table 3) as follows:

$$307 \quad \text{CRPS} = \frac{1}{n} \sum_{i=1}^n \int_{t=-\infty}^{\infty} (F_i^Y(t) - F_i^X(t))^2 dt \quad (4)$$

308 where $F_i^X(t)$ and $F_i^Y(t)$ are, for the i^{th} pixel of the group, the empirical cumulative
 309 distribution functions of the reference (C) rainfall depth ($= 1$ if $x_i \leq t$; $= 0$ otherwise) and
 310 of the ensemble forecasted rainfall depth, respectively. The CRPS allows for the
 311 evaluation of the mean accuracy of an ensemble product while also being sensitive to the
 312 width (precision of the probabilistic product) of the distribution (Hersbach, 2000).

313 Consistency of probabilistic products was evaluated via rank histograms (Talagrand
 314 diagrams). They are drawn for pixels with stratiform rainfall depth between 0.1 and 5 mm
 315 (Group 2, Table 3), for pixels with stratiform rainfall depth larger than 10 mm (Group 4)

316 and for pixels with convective rainfall depth between 0.1 and 5 mm (Group 6). Rank
317 histograms are not well suited for close-to-zero rainfall depths (Groups 1 and 5). Pixels
318 with large convective rainfall depths (Group 7) were of interest, but there were not
319 enough of them for rank histograms. Group 3 (pixels with stratiform rainfall depth
320 between 5 and 10 mm) is not shown for sake of parsimony.

321 **3 Results**

322 **3.1 Deterministic metric: MSE**

323 As illustrated in Equation (3), MSE was broken down in order to verify the mean (bias;
324 Figure 3) and the standard deviation of the error (Figure 4). The results regarding the
325 CaPA-derived products illustrate that GSDM (Cd) reduced bias compared to the low-
326 resolution product Ca, especially for large rainfall depths (Groups 4 and 7). The accuracy
327 (Figure 3) and precision of the error (Figure 4) are also slightly higher for Cd compared
328 to Cdn and even Cn, illustrating the ability of GSDM to generate rainfall depths close to
329 the reference depth at fine scale. Note that all products underestimated the two pixel
330 groups with the largest CaPA rainfall depths.

331 For RDPS forecasts, the bias of the product evaluated with respect to the neighborhood
332 (Rn) was similar, although slightly higher, to that of the raw product (R) (Figure 3). The
333 standard deviation of the error was lower for Rn than for R (Figure 4). In all likelihood,
334 the lower standard deviations for Rn were due to the difference in the MSE calculation
335 method; that is for the mean of the 121 ensemble members for Rn and for the unique
336 deterministic value for R (Table 2). Thus, the standard deviation for Rn is smoothed, but
337 the error of the product is not necessarily more precise. The bias of R was lower than that

338 of the aggregated product (Ra), illustrating the added value of higher spatial-resolution
339 forecasts. In all likelihood, the standard deviation of the error was smaller for Ra than for
340 R, because the former values were spatially smoothed. Biases of the disaggregated RDPS
341 products (Rd and Rdn) were similar to that of the raw product R.

342 Biases for the GEPS-derived forecasts were all very high (Figure 3). The coarse spatial
343 resolution of the raw GEPS product (G) did not lead to smaller and larger intra-tile
344 rainfall depths. The bias of G was larger than that of Ra, which has the same spatial
345 resolution (about 100 km), but built using a forecast with higher spatial resolution
346 (RDPS). Disaggregation (Gd and Gdn) did not provide a way to reduce the bias. As
347 mentioned earlier, a suitable application of GSDM requires an accurate (unbiased), low-
348 resolution, rainfall depth. Obviously, this assumption was not met for GEPS
349 disaggregation.

350 **3.2 Probabilistic metrics: CRPS and rank histograms**

351 Ensembles produced by GSDM from aggregated CaPA analyses resulted in small CRPS
352 values (Figure 5). Again, Cd slightly outperformed Cdn and even Cn; illustrating the
353 ability of GSDM to produce accurate and precise ensemble rainfall depths at fine spatial
354 scale. However, for stratiform events, Cdn outperformed Cd for consistency on pixels
355 with rainfall depths between 0.1 and 5 mm (Figure 6) and larger than 10 mm (Figure 7).
356 This latter figure shows that Cd too often underestimated pixels with large rainfall depths
357 while Cdn did not have this issue. It suggests that GSDM may be not able to put the
358 largest rainfall depths at the exact location, but it can generate these large rainfall depths
359 in a neighboring area. For pixels with convective rainfall depths between 0.1 and 5 mm,
360 consistency of Cd was better (Figure 8).

361 RDPS-derived forecasts had generally smaller CRPS values than those of GEPS-derived
362 forecasts (Figure 5). For RDPS-derived forecasts, CRPS values were almost always
363 smaller for Rd (RDPS disaggregated and evaluated at the target pixel) than for forecasts
364 evaluated at the neighborhood pixels, disaggregated (Rdn) or not (Rn). However, Rd is
365 not consistent for the three groups of pixels analyzed (Figures 6-8). For most of the pixels
366 in each group, the reference value is either smaller than or equal to the first 5% or larger
367 than the last 5% of the stochastic realizations. Rd overestimated too often pixels with
368 stratiform rainfall depths between 0.1 and 5 mm (Figure 6). Rdn had better consistency
369 than Rd, but just slightly lower than Rn (Figures 6-8). That being said, Rn overestimated
370 pixels with convective rainfall depths between 0.1 and 5 mm (Figure 8). It suggests that
371 RDPS produced too smooth forecasts for convective rainfall.

372 For GEPS-derived forecasts, CRPS values for Gd were also smaller than those for Gdn
373 for stratiform rainfalls, but not for convective rainfalls. Consistency was weak for all
374 GEPS-derived forecasts (Figures 6-8), except for Gdn for pixels with stratiform rainfall
375 depths larger than 10 mm (Figure 7).

376 **4 Discussion**

377 The above results demonstrated the capacity of GSDM to generate accurate and precise
378 ensemble rainfall depths at a local scale (10 km) for cases when spatially averaged
379 reference rainfall (Ca) was used as input. The bias and the standard deviation of the error
380 of the disaggregated product Cd always remained smaller than for the low-resolution
381 reference product Ca used as input (Figures 3 and 4). Also, CRPS values for Cd were
382 smaller than the reference ensemble Cn formed from 120 neighboring pixels (+/- 5 in

383 each direction) (Figure 5). However, the disaggregated product Cd was not consistent for
384 stratiform rainfall (Figures 6-7). Including the neighboring pixels in the disaggregated
385 ensemble (Cdn) mitigated the lack of consistency, especially for large stratiform rainfall
386 depths (Figure 7). For convective rainfall (Figure 8), Cd was consistent, thanks to the
387 parameterization of GSDM which adjusts the spatial variability according to CAPE.

388 For the ECCC forecast products analyzed, despite a high bias for large convective rainfall
389 depths (Figure 3), the regional 10-km resolution product (RDPS; R) outperformed the
390 global 100-km resolution ensemble product (GDPS; G) based on accuracy and precision
391 of the error criteria. However, RDPS is a deterministic product and does not provide
392 uncertainty bands for end users. This issue was circumvented by building an ensemble
393 with the RDPS rainfall depths forecasted in the neighboring area (Rn). Rn was relatively
394 consistent for small stratiform rainfall depths (Figure 6), but not as much for large
395 stratiform (Figure 7) and convective rainfall depths (Figure 8). Furthermore, GDPS
396 ensemble was clearly not consistent (Figure 6-8).

397 While the added value of GSDM applied on low-resolution reference rainfall depths is
398 clear, the added value of GSDM applied to ECCC forecasts was difficult to detect.
399 GSDM did not reduce the bias of RDPS and GEPS forecasts (Figure 3). The Rd product,
400 an ensemble at high-resolution (10 km) from the deterministic forecast RDPS, had
401 smaller CRPS values than Rn, an ensemble formed by the raw RDPS rainfall depth in the
402 neighboring pixels (Figure 5). However, consistency of Rd was not as strong compared to
403 that of Rn (Figures 6-8). Including the neighboring pixels in the ensemble forecast (Rdn)
404 increased the consistency. The added value of Rdn compared to Rn was the reduction of
405 the bias for convective events (Figure 8). For GEPS, GSDM did not improve the forecast,

406 except for the consistency of large stratiform rainfall depths, provided that the depths
407 generated in the neighboring pixels be included in the ensemble (Gdn, Figure 7).

408 To summarize, none of the analyzed products provided entirely satisfactory outputs for
409 short-term forecasts. That being said, there is potential for improvements. Integration of
410 a Bayesian approach in GSDM parameter estimation and data assimilation represent one
411 potential improvement. Instead of having the same parameter set for all realizations, the
412 parameter values could be selected from a predefined random distribution for each
413 realization. This would add some randomness to the disaggregated field, while keeping
414 spatial coherence. Similarly, the assumption that the low-resolution rainfall depth used as
415 input is reliable, which is realistic for reanalyses, but not necessarily true in a forecast
416 mode, could be relaxed. Random perturbations could be generated at each realization for
417 the mean areal rainfall depth used as input, as well as for wind speed, wind direction and
418 CAPE values. Finally, neighboring pixels could still be considered, but the number of
419 neighboring pixels could be reduced and/or vary depending on the type of event
420 (stratiform or convective). However, in-depth analyses on the extent of the neighboring
421 area were beyond the scope of this study.

422 From a wider perspective, ongoing improvements of meteorological modeling, including
423 parameterization, data assimilation, spatial resolution, and uncertainty estimation, is at
424 the heart of the matter. With better meteorological forecasts, new goals will become
425 obtainable and spatial disaggregation models or other statistical downscaling techniques
426 will remain of interest. Indeed, these techniques all need accurate input data. This work
427 focused on derived products for end users by coupling GSDM with currently available

428 meteorological products from ECCC. Meteorological model improvement was beyond
429 the scope of this study.

430 **5 Conclusion**

431 A total of 30, 6-h, rainfall events within an area of about 40,000 km² were analyzed to
432 evaluate accuracy, precision and consistency of the Gibbs Sampling Disaggregation
433 Model (GSDM, Gagnon, 2012; Gagnon and Rousseau, 2014) coupled with Environment
434 and Climate Change Canada (ECCC) meteorological short-term forecasts. The goal was
435 to produce reliable information at local scale (10 km) for end users. GSDM ran
436 sufficiently fast to provide an ensemble of rainfall fields for short-term forecasts.

437 Overall, GSDM applied with 100-km aggregated reference rainfall depths as input gave
438 accurate (low bias) and precise (low variability of the error and low dispersion of the
439 ensemble) 10-km fields. For small convective rainfall depths, GSDM was consistent
440 (observed value indistinguishable of a randomly selected realization of the ensemble), but
441 it could be improved for stratiform rainfall depths. When applied in forecast mode,
442 GSDM inherited the bias of the meteorological forecast. In the end, the 10-km
443 disaggregated rainfall depths from 100-km Global Ensemble Prediction System (GEPS)
444 forecasts, which were found to be highly biased and imprecise, resulted in biased and
445 imprecise information.

446 The Regional Deterministic Prediction System (RDPS) provided 10-km rainfall depths
447 with moderate biases. It is worth noting that by aggregating RDPS forecasts to a 100-km
448 spatial scale, biases evaluated on 10-km pixels slightly increased compared to the raw 10-
449 km forecasts, but remained much smaller than those from 100-km GEPS forecasts. The

450 GSDM coupled with 100-km aggregated RDPS forecasts produced better results than
451 with GEPS forecasts. However, despite this improvement, the disaggregated forecasts
452 were not consistent. Including the 120 neighboring pixels in the disaggregated ensemble
453 could help to mitigate the lack of consistency of the forecast, especially for convective
454 rainfall.

455 Possible areas for improvements were identified, such as a Bayesian estimation of GSDM
456 parameters, random perturbations of GSDM inputs and inclusion of a variable number of
457 neighboring pixels in the ensemble, where the exact number could depend on the type of
458 events. These improvements, once ascertained, would remain of interest even if
459 meteorological models were improved.

460 The same analyses for different experimental set ups could produce different outcomes.
461 In the present study, the area was mostly flat, except for the Appalachian Mountains in
462 the south-east portion of the study region. Application in a more complex topographical
463 region could require modifications to GSDM (Gagnon *et al.*, 2013). Also, if one is
464 interested in 6-h rainfall depths at longer lead times (3, 10, 30 days), the meteorological
465 forecast bias and imprecision should increase, resulting in a decrease in the reliability of
466 the disaggregated rainfall depths. This effect could be reduced if one is interested in
467 cumulative rainfall depths instead of a specific 6-h period. Longer time steps would
468 smooth out the spatial variability and might increase the reliability of the forecasts,
469 disaggregated or not.

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600 **Tables**

601 Table 1. Main characteristics of the 30 GEPS events analyzed. The values are the averages from the four 100-km grid cells analyzed
 602 (2 x 2 central grid cells in Figure 2).

Date/Time (UTC)	Rainfall		Wind at 700 hPa		Date/Time (UTC)	Rainfall		Wind at 700 hPa	
	depth (mm/6h)	CAPE (J/kg)	Speed (m/s)	Direction (°)		depth (mm/6h)	CAPE (J/kg)	Speed (m/s)	Direction (°)
2015-07-18 6:00	3.2	1	13.0	223	2015-09-14 6:00	3.2	16	5.9	198
2015-07-18 12:00	5.6	108	14.3	260	2015-09-14 12:00	6.1	5	7.9	100
2015-07-20 0:00	4.7	1475	13.8	273	2015-09-20 6:00	4.6	32	21.7	236
2015-07-26 6:00	4.9	45	12.4	270	2015-09-20 12:00	4.9	0	15.6	253
2015-07-26 12:00	10.0	79	10.3	248	2015-09-30 0:00	9.5	44	13.6	233
2015-07-30 18:00	7.1	593	13.8	238	2015-09-30 6:00	8.1	9	11.2	253
2015-08-04 0:00	4.1	392	15.0	224	2015-09-30 12:00	20.6	0	6.2	238
2015-09-03 12:00	4.2	568	8.4	293	2015-09-30 18:00	11.0	0	4.4	211
2015-09-09 0:00	3.6	305	10.5	239	2015-10-01 0:00	12.8	0	7.8	175
2015-09-10 0:00	4.6	161	13.6	254	2015-10-17 12:00	3.4	0	12.7	238
2015-09-11 12:00	4.1	2	4.9	240	2015-10-25 12:00	6.2	0	23.4	229
2015-09-13 0:00	3.8	56	9.8	223	2015-10-29 0:00	8.2	0	28.9	226
2015-09-13 6:00	8.9	24	10.0	193	2015-10-29 6:00	8.9	0	28.3	219
2015-09-13 12:00	11.4	7	8.3	192	2015-10-29 12:00	14.2	75	21.5	223
2015-09-14 0:00	3.3	154	9.2	197	2015-11-14 0:00	3.22	0	15.1	280

603

604

605 Table 2. Description of the rainfall series analyzed. Raw ECCC products appear in
 606 boldface. For rainfall products aggregated before disaggregation (Cd, Cdn, Rd, Rdn),
 607 wind and CAPE data were aggregated as well.

ID	Source	Resolution	Nr of members of the ensemble
C	CaPA	10 km	1 (deterministic, reference)
Cn	CaPA	10 km	120 neighboring pixels
Ca	CaPA aggregated	100 km	1 (deterministic)
Cd	CaPA aggregated/disaggregated	10 km	100 random realizations
Cdn	CaPA aggregated/disaggregated	10 km	12,100 = 100 random realizations x 121 neighboring pixels
R	RDPS	10 km	1 (deterministic)
Rn	RDPS	10 km	121 neighboring pixels
Ra	RDPS aggregated	100 km	1 (deterministic)
Rd	RDPS aggregated/disaggregated	10 km	100 random realizations
Rdn	RDPS aggregated/disaggregated	10 km	12,100 = 121 neighboring pixels x 100 random realizations
G	GEPS	100 km	21 members
Gd	GEPS disaggregated	10 km	105 = 21 members x 5 realizations
Gdn	GEPS disaggregated	10 km	12,705 = 121 neighboring pixels x 21 members x 5 realizations

608

609

610 Table 3. Groups of pixels on which performance metrics were calculated.

Type of events	Group ID	CaPA rainfall depth (mm)	Number of pixels
Stratiform (CAPE < 500 J/kg)	1	[0, 0.1)	2180
	2	[0.1, 5)	4635
	3	[5, 10)	2000
	4	> 10	1885
Total stratiform			10,700 (111 tiles)
Convective (CAPE > 500 J/kg)	5	[0, 0.1)	742
	6	[0.1, 5)	409
	7	> 5	149
Total convective			1,300 (13 tiles)
Total			12,000 (120 tiles = 30 events x 4 tiles/event)

611

612

613 **Figure Captions**

614 Figure 1. Example of a 6-h rainfall event: depths from the 10-km reference data (left
615 panel), the aggregated 100-km reference data used as input by GSDM (middle panel) and
616 a realization of GSDM at 10-km (right panel).

617 Figure 2. Study area with the 40 x 40 10-km pixels (dotted lines) in the 4 x 4 100-km grid
618 cells (solid lines). The Bécancour watershed is shown for illustrative purposes.

619 Figure 3. Absolute value of the mean error (bias) (i.e. rainfall depth difference with the
620 reference depth C) of all products for the seven groups of pixels. IDs of the rainfall
621 products are defined in Table 2. IDs of the seven groups of pixels are defined in Table 3.

622 Figure 4. Standard deviation of the error of all products for the seven groups of pixels.
623 IDs of the rainfall products are defined in Table 2. IDs of the seven groups of pixels are
624 defined in Table 3.

625 Figure 5. Mean CRPS values of the ensemble products for the seven groups of pixels. IDs
626 of the rainfall products are defined in Table 2. IDs of the seven groups of pixels are
627 defined in Table 3.

628 Figure 6. Rank histograms of each ensemble product for group of pixels 2 (stratiform
629 rainfall depth between 0.1 and 5 mm; 4635 pixels). The dashed line illustrates a rank
630 histogram for a perfectly consistent ensemble product.

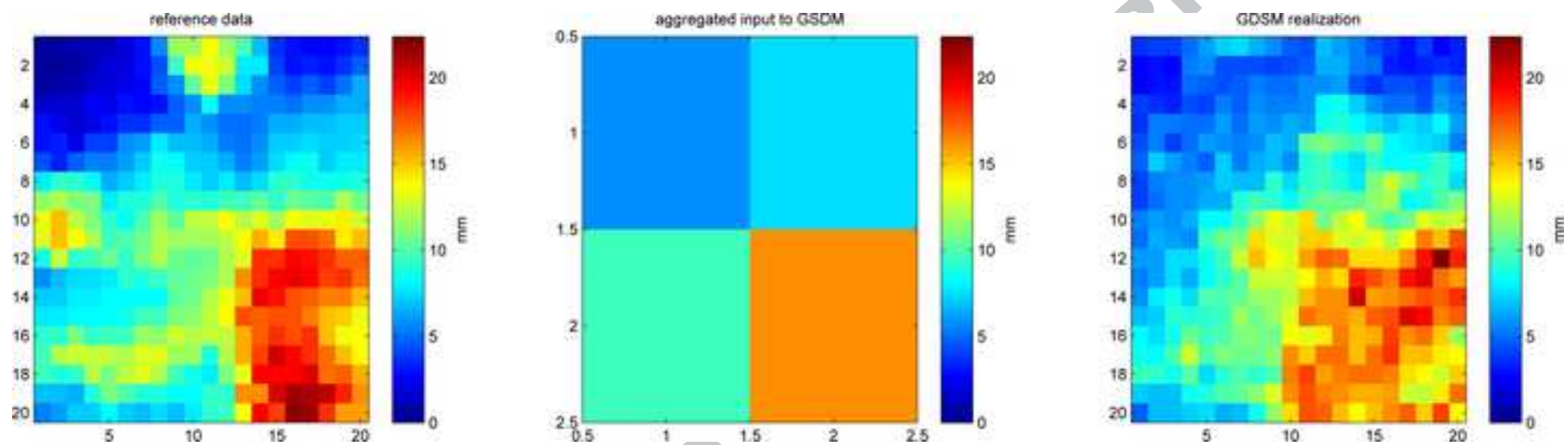
631 Figure 7. Rank histograms of each ensemble product for group of pixels 4 (stratiform
632 rainfall larger than 10 mm; 1885 pixels). The dashed line illustrates a rank histogram for
633 a perfectly consistent ensemble product.

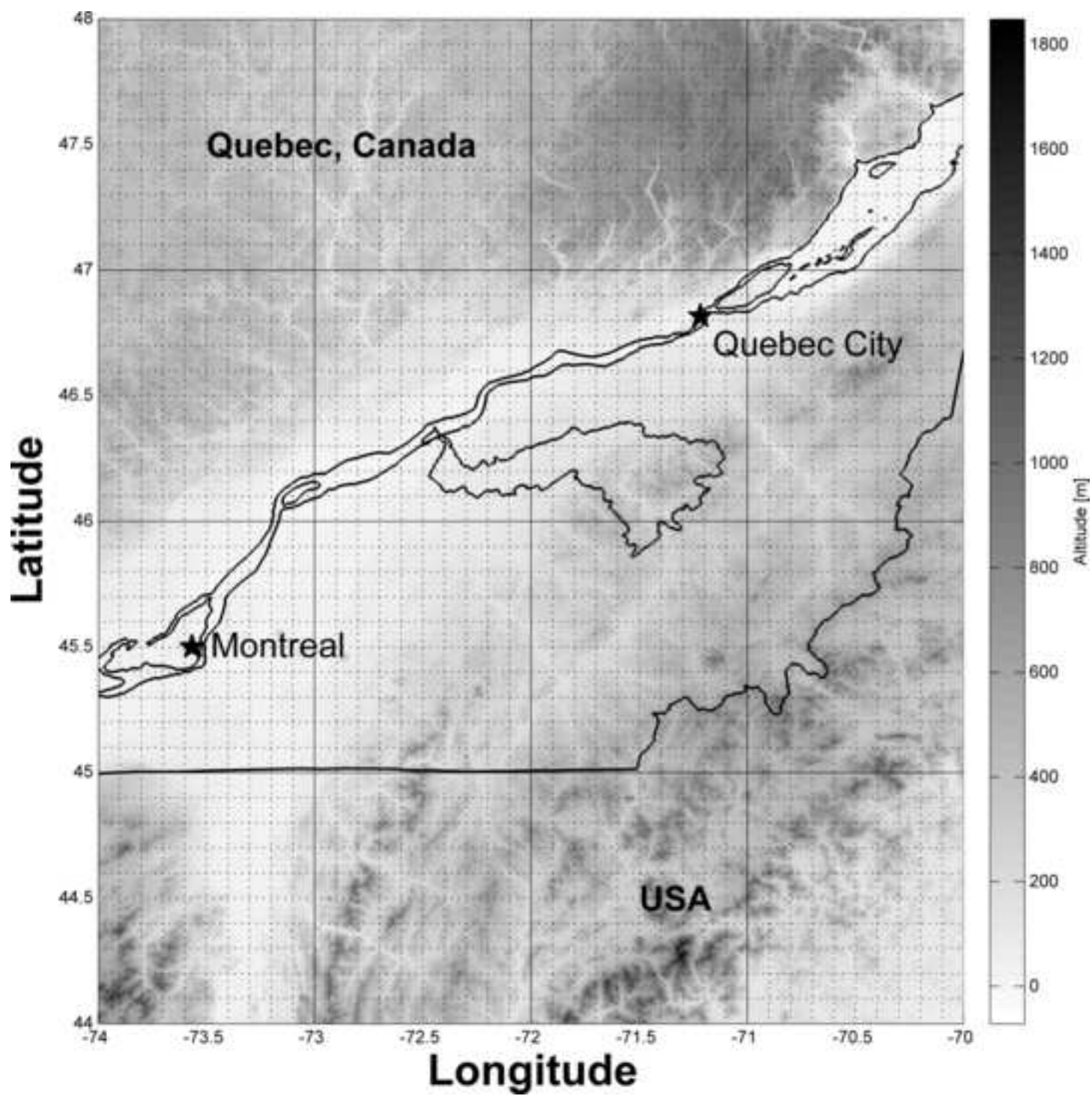
634 Figure 8 Rank histograms of each ensemble product for group of pixels 6 (convective
635 rainfall depth between 0.1 and 5 mm; 409 pixels). The dashed line illustrates a rank
636 histogram for a perfectly consistent ensemble product.

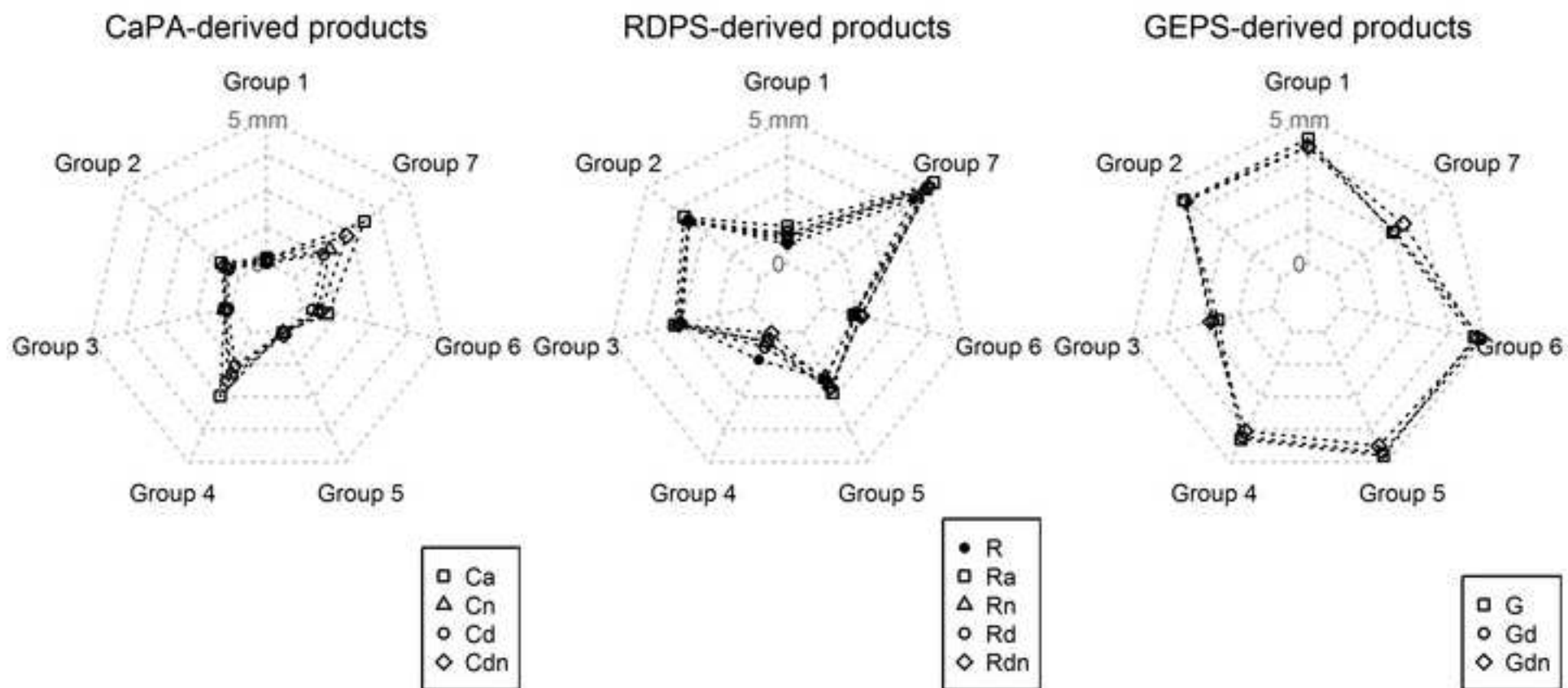
637

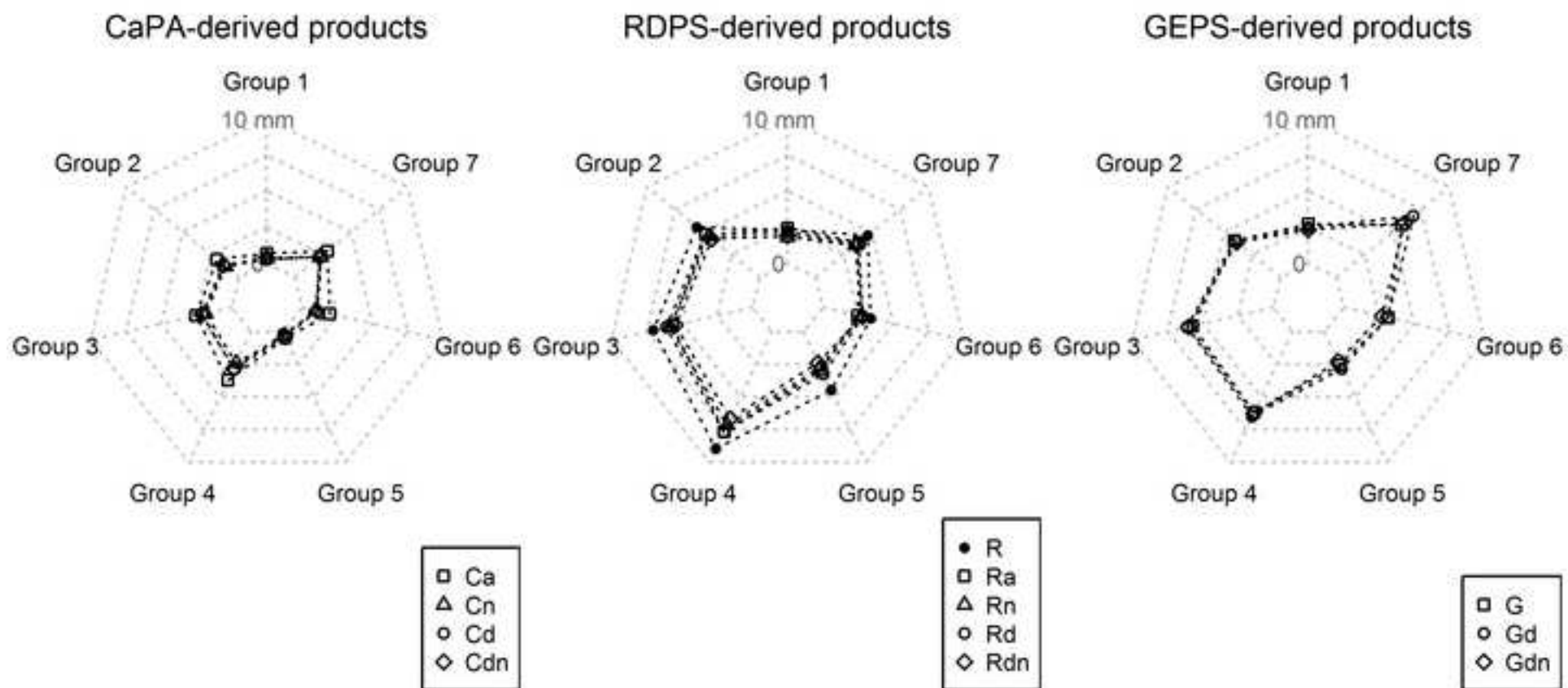
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Figure 1









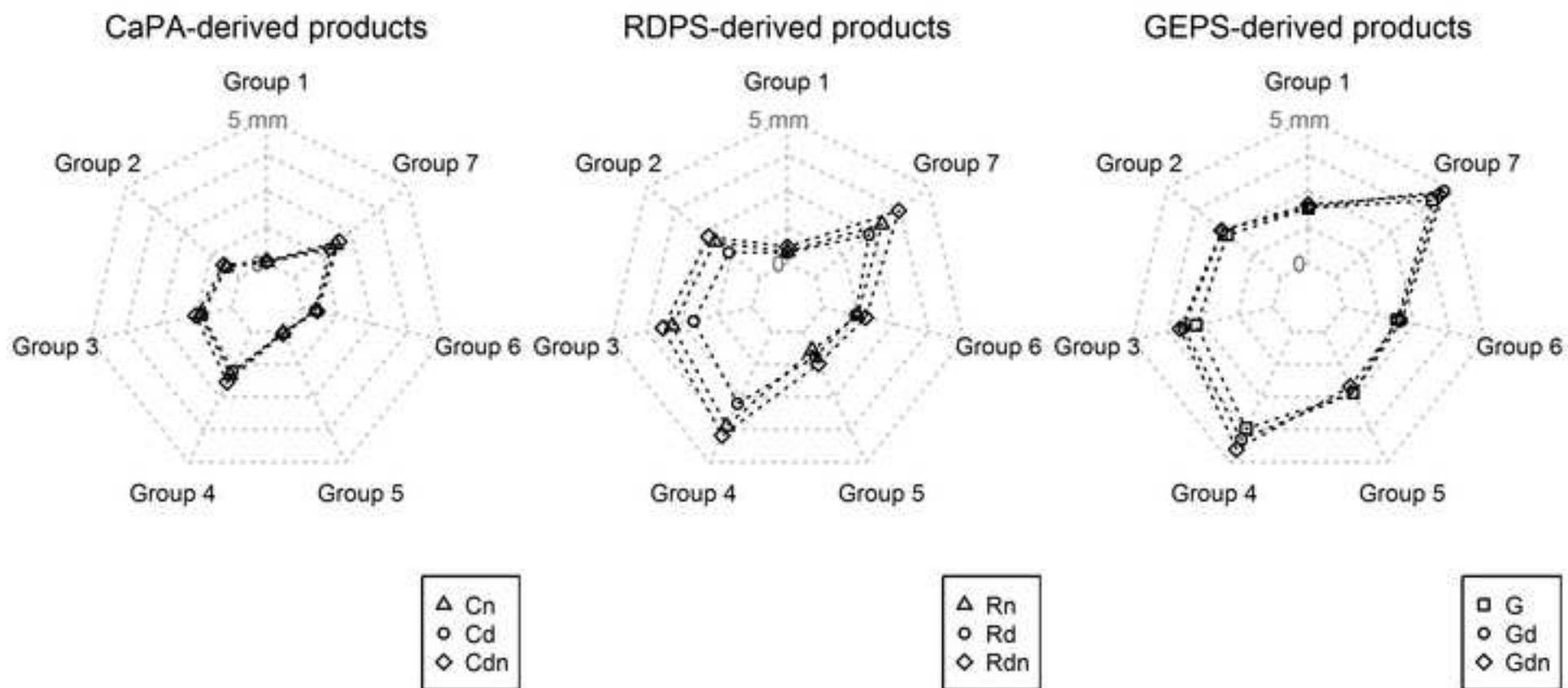
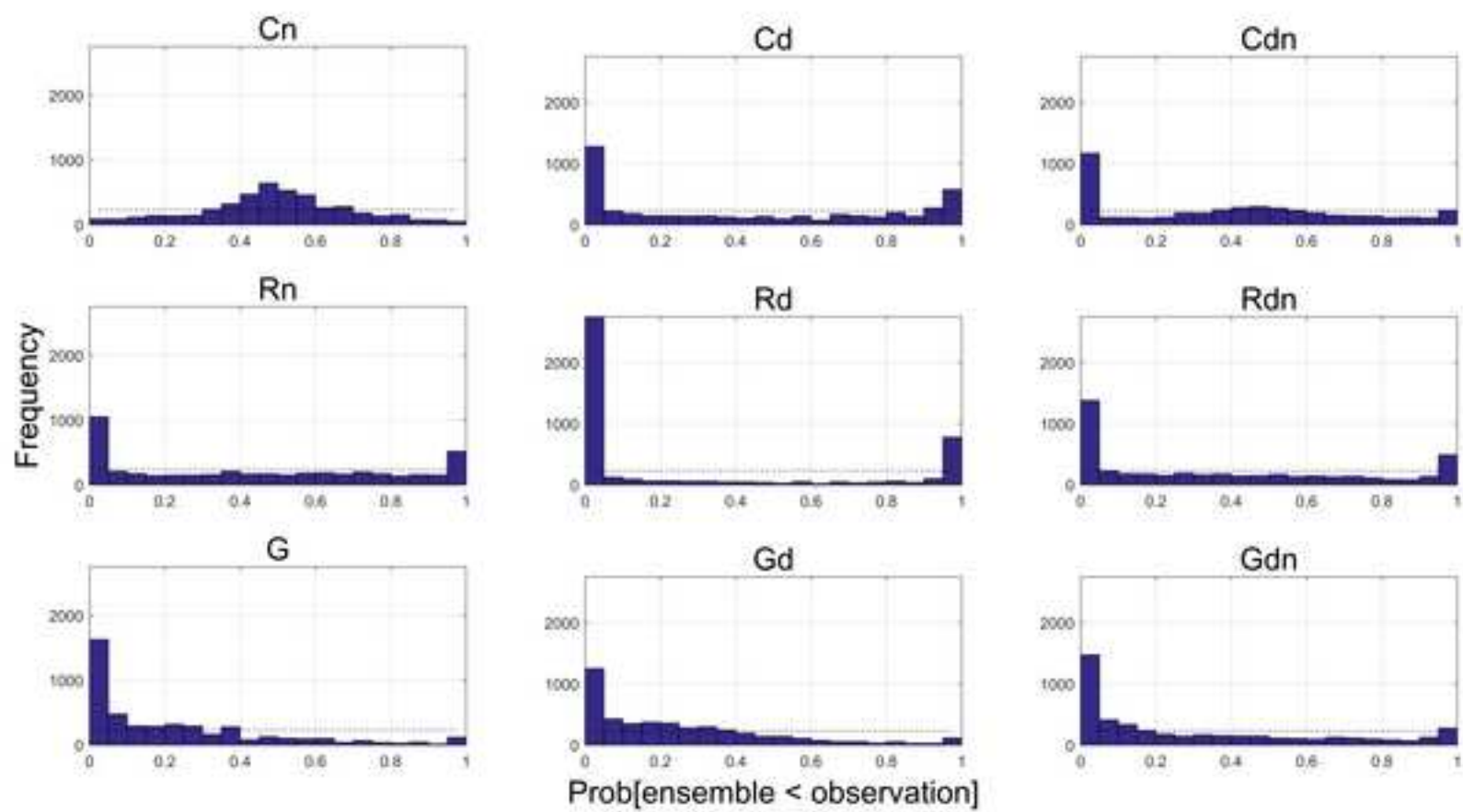


Figure 6



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Figure 7

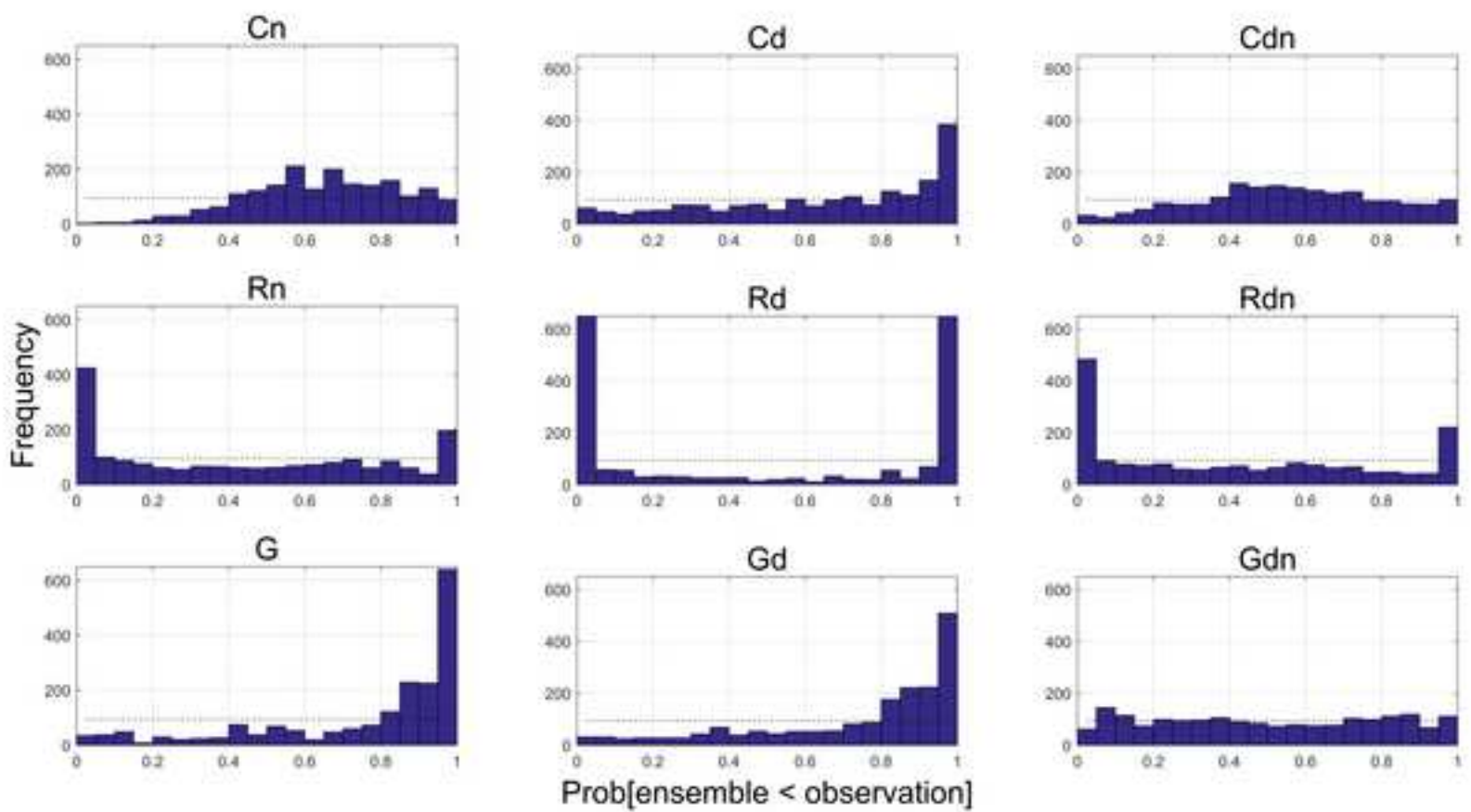
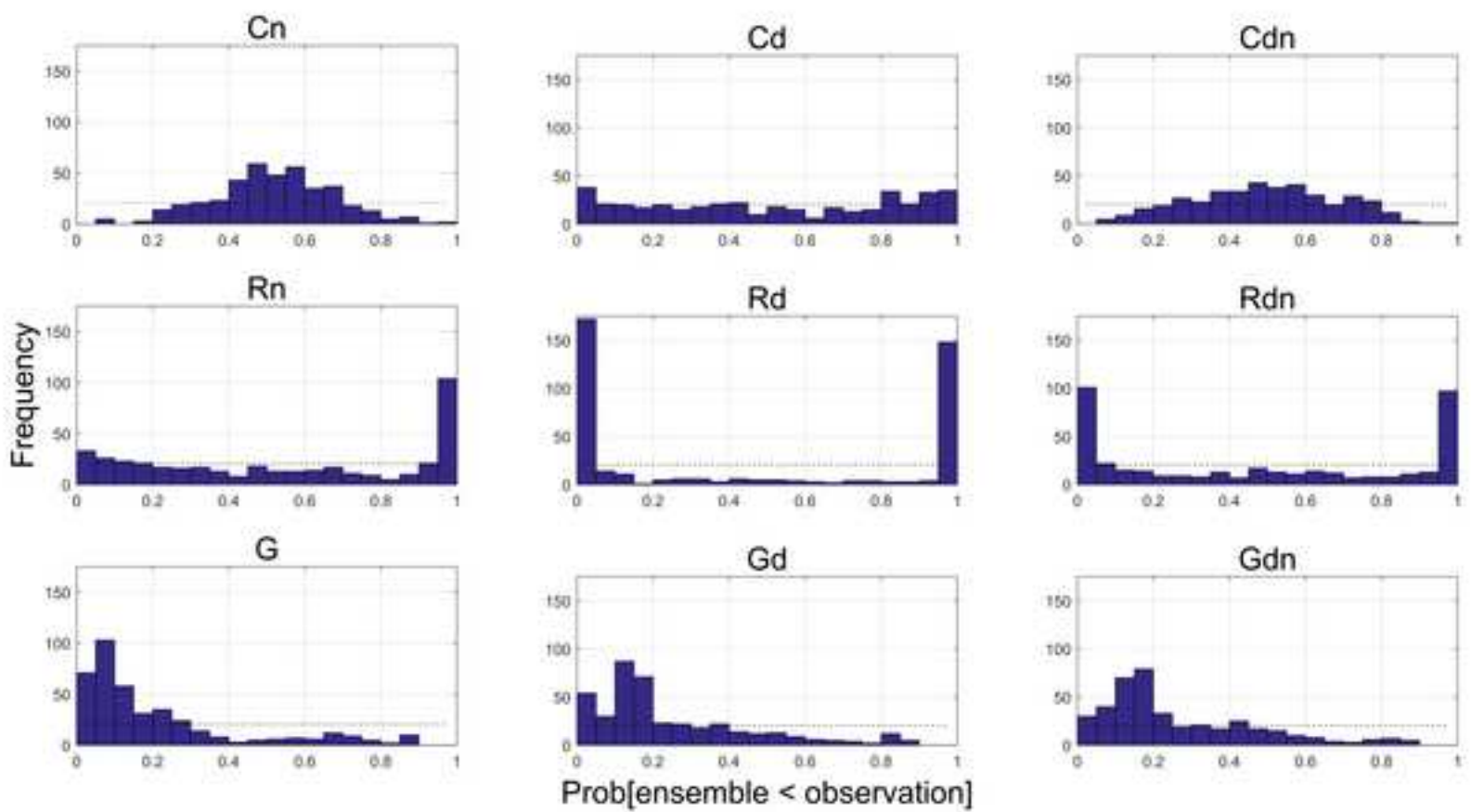


Figure 8



638 **Highlights**

- 639 • GSDM applied on reference data generates accurate and precise rainfall fields
- 640 • GSDM inherits of the forecast bias
- 641 • Global ensemble forecasts (GEPS) are not consistent, with or without GSDM
- 642 • GSDM performance was better with regional deterministic forecasts (RDPS)
- 643 • Neighboring pixels should be considered when producing high-resolution
- 644 ensembles

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