DETECTION OF TREND AND NORM VIOLATION

USER'S MANUAL
"DETECT" and "EXCEED"

Version 2
by
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Mars 1989

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INTRODUCTION

This software package uses non-parametric methods to detect trends in water quality data. Input data may be any compatibly structured temporal series. The program is easy to use due to its interactive and graphic interface.

The principal parts of the program are as follows:

Part 1: Reading of the measured concentrations, mass-loadings and discharges.
Part 2: Graphic representation of the original data.
Part 3: Analysis of sampling frequency, elimination of periods without data (months and/or years), detection of possible seasonality and a concentration - discharge relationship.
Part 4: Choice of a work interval and method to replace missing data, detection of any persistence.
Part 5: Display of inertia graphics (Double-Mass and CUSUM function) from which the type of trend (monotonic or step) may be determined, as well as the date of any change. Recommendation of the most appropriate non-parametric test considering the structure of the present series.
Test: Execution of test and diagnostic.
Part 6: Summary of the data characteristics and the options chosen, as well as parametric interpretation of the results:
- slope of the trend
- date of the change
- initial and final levels
Part 7: Analysis of norm violation.

A flow chart for each of these parts is included in the Appendix.
WARNING

As with all statistical programs of this type, the user is, by his choices, responsible for the validity of the results obtained. Warnings are issued by the program at the various critical steps. Because of changing sampling schemes, the choice of an appropriate work interval requires both that the data collected accurately reflect the phenomenon studied, and that the chosen interval does not create too much fictitious data.
1. General remarks

1.1 System requirements

The program requires an IBM compatible PC, XT or AT model personal computer running DOS 2.0 or higher. It should have:

- 512 K RAM (at least);
- a CGA, EGA or ATT video card;
- a monochrome or color monitor capable of displaying graphics;
- 2 floppy drives, or a hard disk and one disk drive (360 Kb, 5 1/2 in., double sided, double density);
- a dot matrix printer capable of producing graphics;
- an 8087 or 80287 co-processor is not required, but greatly increases calculation speed.

1.2 General information

Although the program can be used on a system with two floppy drives, it was designed to be used with a hard disk, and is therefore more efficient in this configuration.

The program, in its original form, accepts data of maximum length 1390.
1.3 General flow chart

DATA ACQUISITION

DIVISION OF THE FILES

SERIES PREPARATION

GRAPHIC ANALYSES

ANALYSIS OF THE DATA MEASUREMENT

CREATION OF A WORK SERIES

PREPARATION FOR TESTS

TEST

SUMMARY

VIOLATION STUDIES

ACQUISITION

DIV

P1

P2

P3

P4

P5

MW

MWS

KEN

KENS

FS

SP

P6

P7 + P8

CLEAN-UP OF TEMPORARY FILES. TM*

STOP
2. Utilities

To allow more efficient use of the program, several utilities are included. The following is a brief description of these companion programs.

2.1 System_configuration

CONF.EXE

As the program is designed to work on different systems, CONF.EXE allows the user to adapt the program to his particular system characteristics. This program asks questions about the screen resolution, color modes, graphic symbols to use and the definition of the interfaces. The programs can be used with CGA (640 x 200), EGA (640 x 350) and ATT (640 x 400). They can also function in 320 x 200 mode, but certain titles will be superimposed, as the corresponding 40 x 25 text mode does not leave much room for adding comments to the graphs.

CONF.EXE creates the file SETUP.PC which must be present when the programs are used.

N.B. CONF.EXE must be run first, so that the other programs can operate correctly.

2.2 Data_acquisition

ENTRY.EXE

This program permits a simple acquisition of the data, and creates an output file which is easily readable by the file division program. This program also permits the acquisition of a single series of data, which can then be read by P1.

The user is guided by menus and questions which permit him to:
define the presence or absence of dates (the presence of dates is mandatory for the analysis performed by the programs)
- eliminate badly recorded data
- append data to an already existing file

2.3 _File manipulation_

DIVISE.EXE

NAQUADAT and industrial files contain data on concentrations and mass-loadings pertaining to many parameters. This program divides these files into files containing only one parameter.

To use the program, the user types DIVISE with the disk containing the program DIVISE.EXE in the drive. The user is first asked to give the name of the file to be divided, eg. DATA.DAT. The user then is asked to choose one of the three types of files which can be used:

1. Normal NAQUADAT file type
2. NAQUADAT file type with a <CR> after 80 characters
3. Industrial file type

As the two first file types have very spacial uses, the last choice (industrial) will generally be chosen by the user.

This last option allows the treatment of nearly all file types which do not come from NAQUADAT. The user is asked to number the columns in the input file (including the date). He is then guided by menus and explications permitting him to:

- locate the date in the file. Note that if there is no date, the programs can not be used, even if DIVISE.EXE worked. This option is included for the external use of the program when the data are equidistant.
- identify the column containing discharges if one exists.
- transform the concentrations to mg/l, the charges to Kg/day and the discharges to m³/sec so that results from different parts of the program will be compatible.
permit the inclusion of dates, if desired, in the output files. (The dates are mandatory, however, for analysis with the programs).

Finally, the user is asked for output file names. It is not necessary to create files for all the parameters in the input file. For example, only one parameter and one output file may be chosen.
3. Batch files

So that the different parts of the programs can run rapidly and automatically, a series of nested batch files are used. They include: EXCEED.BAT, DETECT.BAT, PP1.BAT, ..., PP5.BAT.

The file EXCEED.BAT permits an analysis of violations, calling successively P1, P2DEP, P7 and P8. The file DETECT.BAT permits a complete trend analysis: P1 ... P6.

Each of the other programs allows the user to restart at a different spot in the programs (for example, PP2 allow the user to restart at P2). However, the proceeding analysis must have been run up to one level farther along than the new starting point. For example, the program can be restarted at PP3 after a complete run of the program, but it could not be started at that point if the execution had stopped at P1.
4. **Series Preparation (P1.EXE)**

This program carries out the following operations:

- completely reads the input file
- identification of the discharges if they exist
- elimination of dates where the studied parameter in question has not been analyzed
- replacement of the sampling date with the number of days since the beginning of the sampling period
- creation of a second quality parameter (concentration or mass-loading) from the discharge series if it exists
- creation of a work file .TMP for later use

**General remarks**

**INPUT FILE**

The input file can contain mass-loadings or concentrations. The data files supplied with the program contain only concentrations. The input file must be in the following FORTRAN format: (12X, I2, 1X, I2, 1X, I2, 16X, F12.6, F12.6), which means:

- 12 spaces
- a 2 digit integer containing the year
- a space
- a 2 digit integer containing the month
- a space
- a 2 digit integer containing the day
- 16 spaces
- a 12 digit real number with 6 decimal places containing the charge or concentration
- a 12 digit real number with 6 decimal places containing the discharge. As this last number is optional, blank spaces should be used if there are no discharges in the file.

**N.B.** The programs can be modified to accept another type of data structure.
The following are examples of files which will be read correctly:

example 1:

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>79-04-19</td>
<td>1.900000</td>
<td></td>
</tr>
<tr>
<td>79-05-10</td>
<td>2.300000</td>
<td></td>
</tr>
<tr>
<td>79-06-07</td>
<td>1.900000</td>
<td></td>
</tr>
<tr>
<td>79-06-29</td>
<td>2.000000</td>
<td></td>
</tr>
</tbody>
</table>

example 2:

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>OOQU02MC920279-04-191440EST 805 25</td>
<td>7.900000</td>
<td></td>
</tr>
<tr>
<td>OOQU02MC920279-05-191550EST 805 25</td>
<td>8.400000</td>
<td></td>
</tr>
<tr>
<td>OOQU02MC920279-06-071200EST 805 25</td>
<td>8.200000</td>
<td></td>
</tr>
<tr>
<td>OOQU02MC920279-06-293400EST 805 25</td>
<td>8.200000</td>
<td></td>
</tr>
<tr>
<td>OOQU02MC920279-08-281300EST 805 25</td>
<td>8.100000</td>
<td></td>
</tr>
</tbody>
</table>

example 3:

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>79-04-19</td>
<td>1.900000 .212341</td>
<td></td>
</tr>
<tr>
<td>79-05-10</td>
<td>2.300000 .198743</td>
<td></td>
</tr>
<tr>
<td>79-06-07</td>
<td>1.900000 .207432</td>
<td></td>
</tr>
<tr>
<td>79-06-29</td>
<td>2.000000 .198672</td>
<td></td>
</tr>
</tbody>
</table>

From the example it is clear that the spaces can be left blank or not, as the fields are not read. This format was chosen because it conforms with that used by NAQUADAT.

**UNITS**

So that quantities agree with those used by the programs, concentration should be in mg/l, mass-loadings in kg/day and discharges in m³/sec.

**DISCHARGE FILE**

If discharges are used, they must be present in the original discharge file and in the file described above.
5. Graphic analysis

This file reads the previously created work file and carries out a graphic analysis. Initially, it presents the temporal evolution of the parameter under study and suggests the elimination of maxima and minima, which, if not rejected as outliers, could bias the graphic interpretation. It should be noted that for the trend detection itself, the choice of non-parametric methods limits the impact of these values.

The program then asks the user if he wants the following plotted:

- Double-Mass curves
- CUSUM function

GENERAL REMARKS

OUTLIERS

Outliers are eliminated so as not to bias the results of the graphic analysis as well as the different parametric analyses carried out in other parts of the program. For the trend detection, the non-parametric tests used yield stable results even if outliers are present. Once such a value has been eliminated, it is no longer accessible by the rest of the program, and the only way to get it back, is to start again with PI using the original file.

DOUBLE-MASS CURVES

Double-mass curves show, using accumulated sums, parameter evolution. For a double-mass curve of the parameter vs. time, we have on the ordinate time $t^*$: $\sum_{t=0}^{t^*} x_t$, où $x_t$ where $x_t$ is the value of the parameter at time $t$. On the abscissa, we have the ranks of time $t^*$ expressed as number of days since the first measured observation. In the case of a double-mass curve of parameter vs. $t^*$ discharge, on the abscissa we would have at time $t^*$: $\sum_{t=0}^{t^*} Q_t$. The ordinate is calculated as in the previous example.
As the observations may not be non-equidistant, the Double-Mass curves should be used here as an exploratory method for detecting trends. Their use in P5 with equidistant data will be more representative of the nature of the phenomenon studied.

What to look for?

A) Double-mass of parameter vs. time

Graphs 2.2 and 2.3 present such Double-Mass curves. The line that starts at (0,0) and goes to the upper right-hand corner of the graph is called the general mean line. Such graph should be regarded as an set of changing slopes. Thus, if a group of points seems to form a straight line with a slope greater than that of the mean line, one can conclude that the mean of these points is greater than that of the mean in general. At the same time, a slope less than that of the mean line means that the mean of these points is less than that of the general mean. These types of curves are therefore very useful for detecting trends in the means.

Other lines, above and below the mean line, can be seen in graphs 2.2 and 2.3. These "rails" represent two standard deviations from the mean line and each is calculated using only the points associated with its side. If these "rails" are far from the mean line, it suggests large variations in the data and allows the detection of large differences between the Double-Mass curve and the mean line. The "rail" is not distinguishable from the mean line if all the points are situated on only one side of it. If there is no trend present, the points of the Double-Mass curve are situated on both sides of the mean line in a random fashion.

B) Double-mass of parameter vs. discharge

The principle of these Double-Mass curves is the same as for parameter vs. time. However, it allows to see if a detected trend vs. time could not have been introduced by an effect of changes in discharges. Therefore, the user should look for a different pattern than that of the Double-Mass of parameter vs. time.
CUSUM FUNCTION

The CUSUM function should be used in the same way as the Double-Mass curves as far as the change of slope of successive points is concerned. The CUSUM function is calculated as follows:

$$\text{CUSUM}(X_t) = \sum_{j=1}^{t} x_j - j \cdot \bar{x}$$

the CUSUM is graphed as a function of time $t$.

What to look for?

The CUSUM function (cumulative sums) in effect rotates the mean lines of graphs 2.2 and 2.3 so that they are brought to the horizontal. The deviations from the general mean line are therefore much more visible as they determine the scale of the graph, in opposition to the mean line as in the double-mass curves.

This graph reveals:

- if the curve intersects the $y=0$ axis very often; in that case there is probably no significant trend
- if there are departures on only one side of the curve, indicating a probable trend
- if the curve is parabolic, suggesting a monotonic linear trend
- if there are discontinuous lines, typical of stepwise trends
5.1 Graphs available

The program can produce up to eight different graphs, although only one is always displayed. It is graph 2.1 which shows the temporal evolution of the parameter and permits the user to see any possible outliers. This graph is displayed after each outlier elimination.

Graphs 2.2 to 2.5 show different Double-Mass curves called by the menu options 1, 2, 3 and 4. These graphs allow the user to detect large deviations on one side of the line representing the general mean (from the lower left to the upper right), these deviations being important in the detection of trends.

Graphs 2.6 to 2.8, the CUSUM curves, allow the user to see, in the form of a trend, the concentration and mass-loadings of the parameter, as well as its associated discharge. These graphs are menu options 5, 6 and 7.

It should be noted that when there are no discharge available, many graphs are not available. If, in a series without discharges, the parameter measured was concentrations, graphs 2.3, 2.4, 2.5, 2.6 and 2.8 will not be available, whereas if mass-loadings was the measured parameter, graphs 2.2, 2.3, 2.4, 2.5, 2.6 and 2.7 will not be available.
6. Series evaluation

This program accomplishes the following tasks:

- display of the temporal evolution.
- establishment of a monthly sampling frequency table. This permits a preliminary evaluation of the work interval. A subsequent question allows the elimination of entire months where sampling did not take place (eg. winter).
- seasonality analysis on a monthly basis (by ANOVA). The resulting graphs of monthly means allow the user to determine a suitable regrouping of the months.
- the detection of a significant concentration-discharge relationship which can be used later if the user wishes.

GENERAL REMARKS

IRREGULAR SAMPLING

As shown in table 3.1, certain questions can be asked if there is irregular sampling.

1. If at least two consecutive months were not sampled. The user is allowed to truncate certain consecutive months. It is not possible to eliminate months which are not adjacent. After months have been eliminated, the only choice of interval which will keep this truncation is one value per month for the non-truncated months. Any other selection will not take into account the previous truncation.

N.B. In using this software, it became evident that the criteria should be a little less restrictive. It is now possible to truncate months if there are two consecutive months with two values or less.
2. If at least one year has less than 4 values, it is possible to limit later analysis. The choices are presented in the following menu:

As the number of values for certain year(s) is small, you may limit the analysis:

1) Eliminate certain intermediate years
2) Eliminate certain months at the extremes
3) Return to frequency table before elimination
4) See the complete table up to now
5) Non-representative distribution: exit without test
6) Normal continuation of program
7) Help

A brief description of the different options follows.

1) Eliminate certain intermediate years

The user is allowed to select certain intermediate years with low frequencies for later analysis. The years which are kept for this analysis must be consecutive. The user will have the choice (in P4) to:

a) use the seasonal means in place of the selected intermediate low frequency years.
b) truncate the selected years
c) do nothing

When b) is selected, a level study (stepwise) before and after the truncation is automatically chosen by the program, using the most appropriate test.
2) Eliminate certain months at the extremes

The user is allowed to choose a smaller analysis period than that defined by the input file. The values which are not part of the newly defined period will be eliminated from the file created by PI (.TMP). Therefore, the rest of the program will treat this series as if the values outside the new period did not exist.

3) Return to frequency table before elimination

This option permits the user to return to the original period if he decides not to keep the newly created one.

4) See the complete sampling frequency table up to now

This option allows the user to see the original table. This is useful when defining a new period.

5) Non-representative distribution: exit without test

This option allows the user to exit the rest of the program if the sampling was too little or irregular. The file SYNTHÈSE.P6 contains the preliminary information about the series, as well as the monthly frequencies (table 3.1). Several criteria in the program's output allow the user to detect a sampling that was too low or too irregular.

6) Normal continuation of program

This option allows the user to return to the normal execution of the program as soon as the data manipulations are finished. The user may also avoid any treatment of years with low frequencies by choosing this option as soon as the menu appears.

7) Help

Gives a bit of help concerning the use of option 1).
ANOVA

The analysis of variance used here is only a preliminary step in the detection of a trend, as it serves only to detect seasonality.

The analyses of variance used in this program use only one value per interval (season) for each year. If the original sample contained more than one observation in the interval, the mean of these values is used.

As little experimental planning was done so as to have optimum results, the analysis of variance must be done with the available data and conclusions validated when they don't seem appropriate. To validate the use of the analysis of variance, a test of the equality of the variances (BARTLETT) is performed before the results are printed, and a warning issued if the equality of the variances is rejected.

SEASONALITY

The analysis of variance is used to construct "seasons" having significantly different means. Firstly, the monthly means are tested to see if they are significantly different. If they are, then there is seasonality. The user is allowed to regroup the data so that larger seasons are analyzed (this option is not possible if months have been truncated). The user can regroup the data as many times as he wishes, however, only the last one will be used. If the user does not regroup, 12 seasons of one month each will be used.

The use of seasons permits the use of tests which take into account the presence of cycles in the data. However, the use of seasonality tests on data with no seasonality, will result in a loss of power as compared to non-seasonality tests.

C-Q RELATIONSHIP

Another way to estimate the values for empty intervals, is to look for a strong relationship between concentration and discharge.
The proposed relationship is of the following form (rating curve):
\[ C = aQ^b \]

Firstly, the following regression is carried out:
\[ \ln C = a^* + b^*\ln Q \]

which results in the initial units of \( a = e^a \) and \( b = b^* \). This model is not the best for the original base, but it is simple and gives a good idea of the strength of the relationship between the concentration and discharge.

6.1 Graphs and tables available

The program contains 5 graphs and 6 tables. However, they will not all be used in any one session, as in many cases there is a different graph or table for either mass-loading or concentration.

A) Graphs

Graphs 3.1 and 3.2 present the temporal evolution of the parameter in question, although only one will be displayed according to whether mass-loading or concentration is being analyzed.

The monthly means for each year for the chosen parameter are plotted on graphs 3.3 and 3.4. The symbols used (1-9) represent the last digit of the year, while the stars connected by straight lines represent the means of all the values for the same month. This graph allows the user to see how the data might possibly be regrouped into homogenous seasons.

Graph 3.5 plots the logs of the concentrations against the logs of the discharges, allowing the user to detect any relationship which might be present between the variables as well as completing the regression analysis presented in table 3.4.
B) Tables

Table 3.1 presents the monthly frequencies of the observation for each year. This allows the user to select an appropriate interval for creating an equidistant series (P4.EXE). When there is sufficiently regular sampling, the mean number of observations per year make the choice of a frequency more easy. This selection should not give rise to too many empty intervals.

Table 3.2 presents the results of the analysis of variance on the equality of the monthly means. Each observation of the original series represents one replicate for the month during which it was taken. The results are presented in the usual form of ANOVA tables:

\[ \begin{array}{cccc}
\text{d.f.} & \text{ss} & \text{ms} & F \\
\end{array} \]

- \text{d.f.} = number of degrees of freedom
- \text{ss} = sum of squares
- \text{ms} = mean square
- \text{F} = value of the statistic for the test \( H_0 : \mu_1 = \mu_2 = \ldots = \mu_{12} \) vs. \( H_1 : \text{the monthly means are not equal} \), where \( \mu_i \) is the mean of the \( i^{th} \) month.

For more information on analyses of variance and their associated hypotheses, refer to NETER and WASSERMAN (1974): Applied Linear Statistical Models. Irwin. Homewood. 842 pp. Seasonality is present if the test shows that the monthly means are significantly different. When the equality of the means is rejected, the user has the option of regrouping the months so as to construct seasons which may be more appropriate.

Table 3.2b presents the results of the analysis of variance of the data regrouped by the user. The table is the same as table 3.2, except that the corresponding test is \( H_0 : \mu_1 = \ldots = \mu_k \), where \( k \) is the number of seasons defined when the data were regrouped. Tables 3.3 and 3.3b are used if the parameter analyzed was mass-loading instead of concentration.

Table 3.4 presents the results of the regression in the form of the relationship \( C = aQ^b \). The first results, variance and mean, are the natural logs of the concentration and discharge. The parameter estimators \( a \) and \( b \) are
obtained from the result of the regression $C = a^* + b^* \ln Q$, transforming $a = e^{a^*}$ and $b = b^*$. The percentage of the variance explained gives an estimate of the strength of the relationship. FISHER's test is also used to determine if the relationship is significant and to allow a valid estimate of the concentrations from discharges.
7. Work series, creation and structure (P4.EXE)

This part of the program carries out the following:

- choice of an interval
  - days (1, 3, 7, 15)
  - month (1, 2, 3, 4, 6, 12)

- replace missing values using one of three methods:
  a) temporal interpolation
  b) seasonal mean
  c) concentration-discharge relationship

At this stage, a complete series of equidistant values has been generated and saved in files with extensions .TMC or .TML, depending on whether they are concentrations or mass-loadings.

The last part of this program determines if there is persistence, and if there is, whether it is Markovian.

GENERAL REMARKS

GENERATION OF MISSING VALUES

The choice of a work interval which is too small will result in the creation of fictitious data (generation of missing values). It is important not to fill in too many intervals with the available methods (seasonal means, interpolation, concentration-discharge relationship). In order to make the user aware of this situation, a warning is issued when more than 20% of the intervals will be synthetised using other data. The user can then choose another interval so as to reduce the number of intervals without data, or he can continue, knowing that the chosen work series contains a large percentage of fictitious data (in certain cases, the sampling may have been very irregular, making a better choice of interval difficult).
METHODS OF GENERATING DATA FOR EMPTY INTERVALS

The three methods offered for the creation of data are:

- Temporal interpolation.
- Use of the mean value of the parameter taken in the same period in the other years.
- Use of concentration-discharge relationship.

Interpolation is used when there is no seasonality, but there is persistence. It should be noted, however, that the use of this method will increase the persistence.

The use of the mean value for the interval during the other years is done when seasonality is present and when representative means of each of the intervals is used.

The concentration-discharge method is the preferred method, but it is not very often that the relationship is strong enough to allow a valid estimate for the empty interval.

N.B When the number of observation is low, it may be better to choose the second method (means) so as not to create persistence before it is studied. In fact, there is a difficulty in the analysis: equidistant data should be used for the analysis of persistence lent a preliminary persistence analysis could validate the interpolation as the method for data generation.
7.1 Tables available

The program has two tables. Table 4.1 displays the number of missing values per interval: the number of intervals is the number of complete intervals in a year. Intervals are numbered from the beginning of the calendar year, if there has been no truncation. The number of missing values for an interval is the number of years for which there was no observation available for that interval. If the number of missing values is high for all the intervals, it is probably because the interval chosen was too narrow (frequency too high). On the other hand, few missing values may mean that the interval was well chosen in the case of regular sampling, or that the chosen interval was too large (low frequency). It should be noted that this table will not be presented if there were no missing values (no empty intervals).

Table 4.2 displays the results of the analysis of persistence done on the equidistant series. The coefficients of correlation for the first to sixth order, and their associated standard deviations, are presented. From this, the user can see the coefficients that were significantly different from 0 as well as the most probable structure of the persistence (as determined by the program). Three different structures can be identified. In the first, there is no persistence (the first order autocorrelation coefficient ($\rho_1$) is not significantly different from 0). The second structure is Markovian persistence ($\rho_1$ is significantly different from 0 and the second order partial autocorrelation coefficient is not significantly different from 0). Finally, the third is non-Markovian persistence ($\rho_1$ and the second order partial autocorrelation coefficient are significantly different from 0).

A coefficient is considered significantly different from 0 if its value is at least 2 times greater than its standard deviation.
8. Test preparation (P5.EXE)

This program gathers together all the information about the work series that has been determined by the preceding programs: interval, seasonality, persistence, length, etc.

It then determines which part of the series to analyze, if there is a monotonic or step trend, and suggests the appropriate test according to the following decision tree:

<table>
<thead>
<tr>
<th>TREND</th>
<th>PERSISTENCE</th>
<th>SEASONALITY</th>
<th>APPROPRIATE TEST</th>
</tr>
</thead>
<tbody>
<tr>
<td>Monotonic → trend</td>
<td>Markovian</td>
<td>- no seasons</td>
<td>Lettenmaier/Spearman</td>
</tr>
<tr>
<td></td>
<td>persistence</td>
<td>- with seasons</td>
<td>Hirsch and Slack</td>
</tr>
<tr>
<td></td>
<td>No</td>
<td>- no seasons</td>
<td>Spearman/Kendall</td>
</tr>
<tr>
<td></td>
<td>persistence</td>
<td>- with seasons</td>
<td>Kendall seasonality</td>
</tr>
<tr>
<td>Stepwise → trend</td>
<td>Markovian</td>
<td>- no seasons</td>
<td>Lettenmaier/Mann-Whitney</td>
</tr>
<tr>
<td></td>
<td>persistence</td>
<td>- with seasons</td>
<td>Hirsch and Slack</td>
</tr>
<tr>
<td></td>
<td>No</td>
<td>- no seasons</td>
<td>Mann-Whitney</td>
</tr>
<tr>
<td></td>
<td>persistence</td>
<td>- with seasons</td>
<td>Kendall seasonality</td>
</tr>
</tbody>
</table>

The test chosen by the user is carried out and the results displayed.

GENERAL REMARKS

MONOTONIC OR STEPWISE?

The choice of the detection of a monotonic or stepwise trend can be made according to the knowledge the user has about the series under study. The objective of the analysis also helps in making the choice. For example, if one wants to study the impact of the opening a treatment plant, it would be best to choose detection of stepwise trend with the separation on either side of the
opening date of the plant. For those cases where the changes are more gradual, such as the acid rain effect or changes of land uses in a watershed, the monotonic trend detection should be used.

When the trend is very strong, either method will work while the criteria for model adjustment at the end of P6 can be used to choose the most appropriate test. The CUSUM functions can be very useful from an exploratory point of view when making such a choice. In fact, a stepwise trend results in a CUSUM of the form:

![CUSUM graph for stepwise trend]

while the CUSUM of a monotonic trend looks like:

![CUSUM graph for monotonic trend]

The two models can be identified from these graphs, making the choice easier.
DOUBLE-MASS AND CUSUM

These graphs should be considered in the same way as in P2. The data, however, are now equidistant permitting a more efficient study of the graphs.

It is important to use the graphs in a complementary fashion: the double-mass graph gives a idea of the amplitude of the possible trend, while the CUSUM graph gives a better idea of the changes in the slope. In fact, the height of the Double-Mass is defined by the extreme right of the cumulated values, and large deviations from that line are a hint for the significance of the trend. The height of the CUSUM graph is defined by the amplitude. Therefore, it will always appear that there is a significant trend, so the CUSUM must be used to appreciate changes in slopes.

ANOTHER TEST?

In general, the test suggested above is the most appropriate, but in certain cases the user may want to compare the results with those of other tests. When a Markovian persistence is detected, the suggested tests use the LETTENMAIER correction for Markovian persistence. The user may want to compare the results obtained with this adaptation, with those obtained without it, to see if there is a difference in trend detection.

For various reasons, the analysis of seasonality may not be convincing due to the presence of outliers which make the distribution of the data non-normal (the equality of the variances may be rejected). In this case, the user may want to compare the results of seasonal tests with those of non-seasonal tests.

The agreement of several tests permits the validation of the conclusions despite factors such as persistence and seasonality. When there is no agreement, the user must use his best judgement to determine the best test to use in the face of the effects of seasonality or persistence.

It may also be advisable to choose another test if the suggested test is seasonal and there are few observations. This is especially important in the case of the MANN-WHITNEY seasonality test as its power is not known and the data used must have been taken before and after a separation.
8.1 Graphs available

The program contains four graphs, although only two will be displayed for any analysis according to whether the user has chosen to analyze concentrations or mass-loadings.

Graph 5.1 displays the double-mass curve of the parameter concentration as a function of time. This graph is made from the equidistant series, and it is this difference that distinguishes it from graph 2.2. The trend structures, however, are the same type. Graph 5.2 is displayed when the mass-loading is analyzed instead of the concentration.

Graph 5.3 displays the CUSUM curve of the parameter concentration in function of time. The equidistant series is used for this graph as well. This graph allows the user to detect break points, which can serve as separation points in the case of a Mann-Whitney test for the detection of a stepwise trend. Graph 5.4 is displayed when mass-loading is analyzed instead of concentration.
9. Tests

Twelve tests are available to the user. The majority of these tests are classic non-parametric tests modified so that they take into account seasonality and/or persistence. Six programs allow the different tests to be run on regrouped data so that each program runs the test for the case where persistence is present and a corresponding test where persistence is absent.

Table 9.1 displays the number and name of each test as well as the program where it is located:

Table 9.1: Tests available

<table>
<thead>
<tr>
<th>Test number</th>
<th>Test name</th>
<th>Program name</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>MANN-WHITNEY</td>
<td>MW.EXE</td>
</tr>
<tr>
<td>2</td>
<td>MANN-WHITNEY/LETENMAIER</td>
<td>MW.EXE</td>
</tr>
<tr>
<td>3</td>
<td>MANN-WHITNEY/SEASONALITY</td>
<td>MWS.EXE</td>
</tr>
<tr>
<td>4</td>
<td>MANN-WHITNEY SEAS/LETENMAIER</td>
<td>MWS.EXE</td>
</tr>
<tr>
<td>5</td>
<td>KENDALL</td>
<td>KEN.EXE</td>
</tr>
<tr>
<td>6</td>
<td>SPEARMANN/LETENMAIER</td>
<td>SP.EXE</td>
</tr>
<tr>
<td>7</td>
<td>KENDALL SEASONALITY</td>
<td>KENS.EXE</td>
</tr>
<tr>
<td>8</td>
<td>HIRSCH AND SLACK</td>
<td>KENS.EXE</td>
</tr>
<tr>
<td>9</td>
<td>FOSTER AND STUART 1</td>
<td>FS.EXE</td>
</tr>
<tr>
<td>10</td>
<td>FOSTER AND STUART 2</td>
<td>FS.EXE</td>
</tr>
<tr>
<td>11</td>
<td>KENDALL'S TAU</td>
<td>KEN.EXE</td>
</tr>
<tr>
<td>12</td>
<td>SPEARMAN</td>
<td>SP.EXE</td>
</tr>
</tbody>
</table>

All the information on the construction and application of these tests is in the detailed methodological report of the programs. Technical specifications are presented for each.
10. **Analysis summary (P6.EXE)**

This program summarises all the results obtained for the series and presents, for the parametric tests, the dates of the changes, the levels of the parameter studied as well as the slopes of the trends.

**GENERAL REMARKS**

**CRITERIA ADJUSTMENT**

The criteria adjustment and the graphic study at the end of P6 allow the user to judge how well the trend model used (stepwise or monotonic) was suited to the data. The smaller the root mean square error (RMSE), the better the adjustment. The elimination of extreme values in P2 will generally reduce the RMSE, but should not be used for this purpose.

**PARAMETRIC VS. NON-PARAMETRIC**

As the trend detection tests used in this software package are all non-parametric and the analyses in P6 are all parametric, there can occasionally be disagreement between results. In such cases, the presence of extreme values is usually the cause of the contradictory results. The user can restart the program at P2 and eliminate the extreme values if agreement of the results is desired. Such a phenomenon is possible because of the weak influence of outliers on non-parametric tests compared to parametric tests. It is always preferable to give more weight to the results obtained with the non-parametric results.
Several distinct outputs are available according to the presence of seasonality and the type of trend studied. All output in text mode is written to the screen and a file (SYNTHESE.P6) at the same time; each time it is run, results are appended to the end of this file.

The only difference between what is seen on the screen and what is written to the file SYNTHESE.P6 is the screen display of the graphs showing the quality of the adjustment for the type of trend chosen (none, monotonic or stepwise). In the case where there is no trend, only the general mean is plotted as a straight line.
11. NORM VIOLATION (P7.EXE AND P8.EXE)

This program studies the frequency, intensity and the duration of those values of a series (concentrations or mass-loadings) which exceed an environmental norm or regulation. It also allows the comparison of two sub-populations from the studied series. The definition of the two sub-populations can be determined after completion of the preceding program (DETECT) (before and after the first operation of a treatment plant, for example), or completely arbitrarily (recent data vs. old data, summer months vs. winter months, high-flow data vs. low-flow data). In any case, it is only necessary to run the preparation program P1.

11.1 Definition of the sub-populations

The sub-populations are divided by boolean intersections according to dates (start-end), specific months or classes of discharge.

11.2 Choice of a norm or threshold

Once the sub-populations are defined, the user must choose a norm or reference. Three norms are available:

a) A general or individual norm which should never be exceeded. It applies to each value of the populations used.

b) A monthly norm which is applied to the monthly means of the values used.

c) An individual norm which can be exceeded once per month. It is applied to each value of the populations used, the highest value, if exceeding the norm for each month, being eliminated.
11.3 Analysis

Once the form of the analysis has been chosen, the program calculates and prints the results for each sub-population (individual or monthly):

- number of values present
- mean
- standard deviation
- median
- number of violations
- percentage of violations

A table then displays the statistics concerning the duration of the violations in each of the sub-populations:

- duration of violation and associated frequency
- mean duration of the violations
- associated standard deviation

A series of graphs is then displayed which compare the distributions and cumulative distributions of the two chosen populations. This is followed by graphs which compare the violations of each sub-population, with values which exceed the norm plotted relative to the chosen norm. Finally, a graph showing the duration of successive violations is displayed.

As with program P6, program P7 writes the results of the analyses to a file. In this case, it writes to SYNTHESE.P7, and as before, each time the program is run, results are appended to the end of the file.

In addition, during the execution of P7, graphs are displayed on the screen, and will be printed if the user has selected this option in P1.
FLOW-CHART OF PROGRAM P1

READING OF C OR L

DO DISCHARGES EXIST?

yes

READING OF DISCHARGES

creation of the second data file

creation of file .tmp

analysis of
0- concentration
1- mass-loading

graph on printer?

yes

print = 1

no

print = 0

stop
FLOW-CHART OF PROGRAM P2

GRAPH OF SERIES VS. TIME

REJECT OF MAX AND/OR MIN AS OUTLIERS?

yes

no

LEGEND

C = CONCENTRATIONS
L = MASS-LOADINGS
T = TIME

1
2
3
4
5
6
7
8
9

1-7

1
2
3
4
5
6
7
8
9

STOP
FLOW-CHART OF PROGRAM P4

SEASONALITY DETECTED IN P3 ?
  yes
  ↓
DO YOU WANT THIS REGROUPING ?
  no → DETERMINATION OF WORK INTERVAL
  yes
  ↓
CREATION OF CORRESPONDING INTERVAL
  ↓
TABLE OF MISSING VALUES
  ↓
PERSISTENCE STUDY
  ↓
$P_1$ SIGNIFICANT
  no → IPERS=0, RHD=0
  yes → IPERS=1, RHD=$P_1$
  ↓
STOP
FLOW-CHART OF PROGRAM P5

DOUBLE-MASS CURVE

CUSUM CURVE

TREND TYPE? STEPWISE OR MONOTONIC

SERIES DIVISION? yes ASK FOR RANKS OR DATES FOR DIVISION

no

SUGGESTED TEST ACCORDING TO TYPE OF TREND, PERSISTENCE AND SEASONALITY

no

CHOICE OF THE TEST TO USE

USE OF THE APPROPRIATE TEST?

yes

WRITING OF INFORMATION TO IDENT.TMP FOR USE BY TEST

STOP
FLOW-CHART OF PROGRAM P6

DISPLAY OF GENERAL INFORMATION ABOUT THE SERIES

\[
\begin{align*}
\text{DISPLAY OF} & \quad \bar{x}_T, \sigma_T \\
\text{DISPLAY OF} & \quad x_s, \sigma_s, s=1 \ldots S \\
\end{align*}
\]

HAS A TREND BEEN DETECTED BY THE TEST? no

yes

STEPWISE TREND

MONOTONIC TREND

SEASONALITY?

SEASONALITY

no

yes

DISPLAY OF

\[
\begin{align*}
\text{DISPLAY OF} & \quad \bar{x}_T, \sigma_T \\
\text{DISPLAY OF} & \quad \bar{x}_s, \sigma_s, s=1 \ldots S \\
\end{align*}
\]

BÉFORE AND AFTER THE STEP

DISPLAY OF

- MEAN SLOPE
- INITIAL AND FINAL LEVELS

DISPLAY OF

- MEAN SLOPE FOR THE GLOBAL SERIES AND EACH SEASON
- INITIAL AND FINAL LEVELS

STOP

\[\bar{x}_T = \text{MEAN OF THE GLOBAL SERIES}\]
\[\sigma_T = \text{STANDARD DEVIATION}\]
\[\bar{x}_s = \text{SEASONAL MEAN}\]
\[\sigma_s = \text{SEASONAL STANDARD DEVIATION}\]
\[S = \text{NUMBER OF SEASONS}\]
FLOW-CHART OF PROGRAM P7-P8

CHOICE OF SUB-POPULATIONS
- dates
- months
- discharges

CHOICE OF A NORM
- individual
- monthly
- once per month

STATISTICAL ANALYSIS OF THE SUB-POPULATIONS

STUDY OF THE FREQUENCY, INTENSITY AND DURATION OF THE VIOLATIONS

GRAPHS COMPARED FOR THE SUB-POPULATIONS

SUMMARY

ANOTHER TYPE OF NORM TO ANALYSE?
- yes
- no

STOP